

# Definitions of profile and flank line modifications and manufacturing deviations in KISSsoft

1.6.2022, for 2022 release

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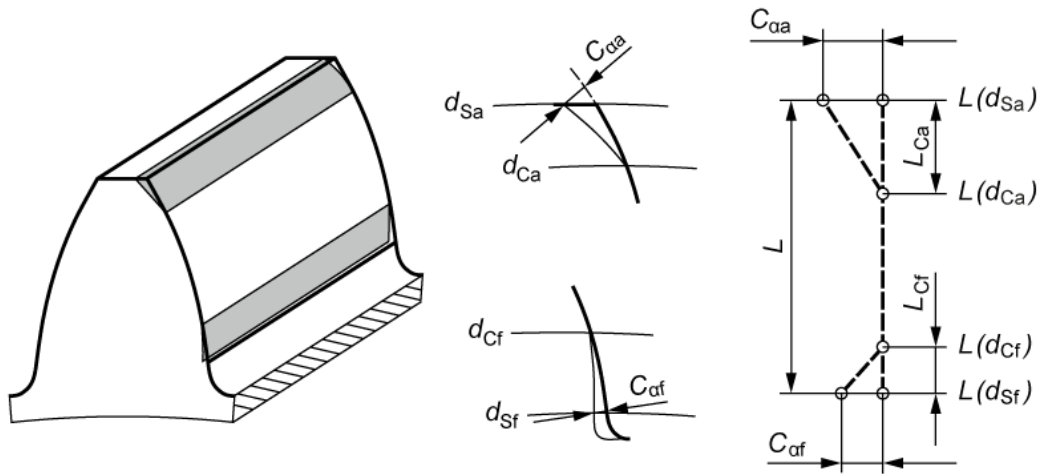
## CHANGE LOG

Date	Person	Change

# 1 Profile and flank line modifications

## 1.1 Tip and root relief, linear

Picture: Mod\_tipRootReliefLinear.png

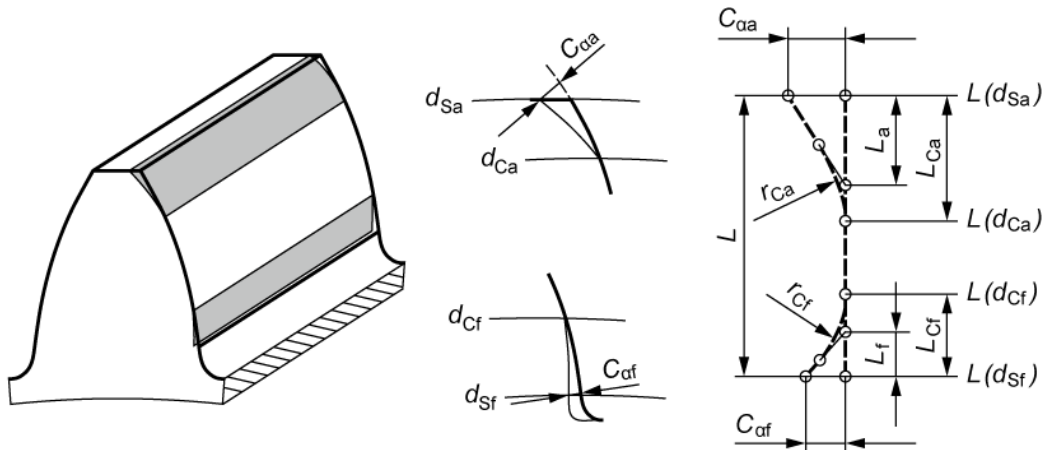


$d_{s_a}$	tip relief, start, at tip	$d_{s_f}$	root relief, start, at root
$d_{c_a}$	tip relief, end, at tip	$d_{c_f}$	root relief, end, at root
$C_{a_a}$	tip relief, value, normal to involute	$C_{a_f}$	root relief, value, normal to involute
$L_{C_a}$	tip relief, roll length	$L_{C_f}$	root relief, roll length
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{a_a}, C_{a_f}$	$L_{C_a}/m_n, L_{C_f}/m_n$	-
<b>Conditions</b>	$\neq 0$	$> 0$	-

## 1.2 Tip and root relief, linear with transition radius

Picture: Mod\_tipRootReliefRad.png

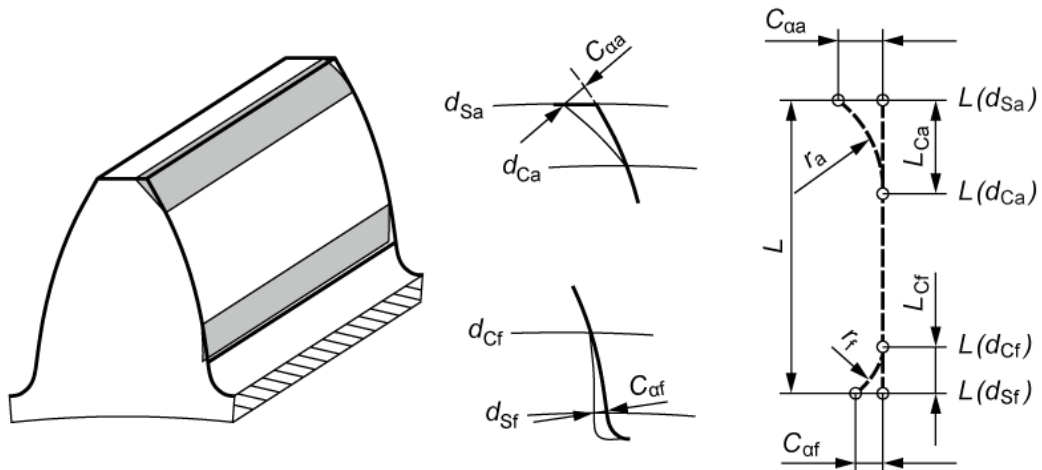


$d_{Sa}$	tip relief, start, at tip	$d_{Sf}$	root relief, start, at root
$d_{Ca}$	tip relief, end, at tip	$d_{Cf}$	root relief, end, at root
$C_{aa}$	tip relief, value, normal to involute	$C_{af}$	root relief, value, normal to involute
$L_{Ca}$	tip relief, roll length	$L_{Cf}$	root relief, roll length
$r_{Ca}$	transition radius, at tip	$r_{Cf}$	transition radius, at root
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa}, C_{af}$	$L_{Ca}/m_n, L_{Cf}/m_n$	$r_{Ca}/m_n, r_{Cf}/m_n$
<b>Conditions</b>	$> 0$	$> 0$	$> 0$

### 1.3 Tip and root relief, arc like

Picture: Mod\_tipRootReliefArc.png

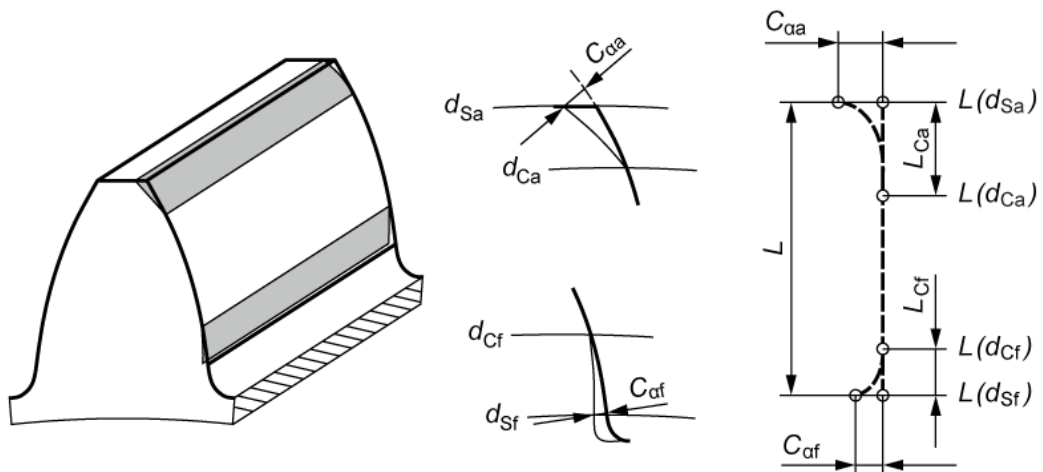


$d_{sa}$	tip relief, start, at tip	$d_{sf}$	root relief, start, at root
$d_{ca}$	tip relief, end, at tip	$d_{cf}$	root relief, end, at root
$C_{aa}$	tip relief, value, normal to involute	$C_{af}$	root relief, value, normal to involute
$L_{ca}$	tip relief, roll length	$L_{cf}$	root relief, roll length
$r_a$	tip relief, radius	$r_f$	root relief, radius
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa}, C_{af}$	$L_{ca}/m_n, L_{cf}/m_n$	-
<b>Conditions</b>	$\neq 0$	$> 0$	-

## 1.4 Tip and root relief, progressive

Picture: **Mod\_tipRootReliefProg.png**

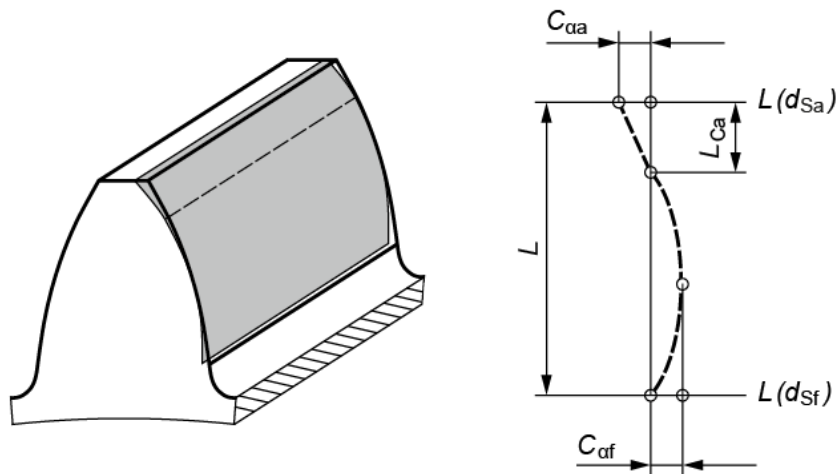


$d_{sa}$	tip relief, start, at tip	$d_{sf}$	root relief, start, at root
$d_{ca}$	tip relief, end, at tip	$d_{cf}$	root relief, end, at root
$C_{aa}$	tip relief, value, normal to involute	$C_{af}$	root relief, value, normal to involute
$L_{ca}$	tip relief, roll length	$L_{cf}$	root relief, roll length
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa}, C_{af}$	$L_{ca}/m_n, L_{cf}/m_n$	see manual
<b>Conditions</b>	$\neq 0$	$> 0$	$5 < \text{Factor 2} < 20$

## 1.5 Tip relief, linear with profile crowning

Picture: Mod\_tipReliefCrown.png

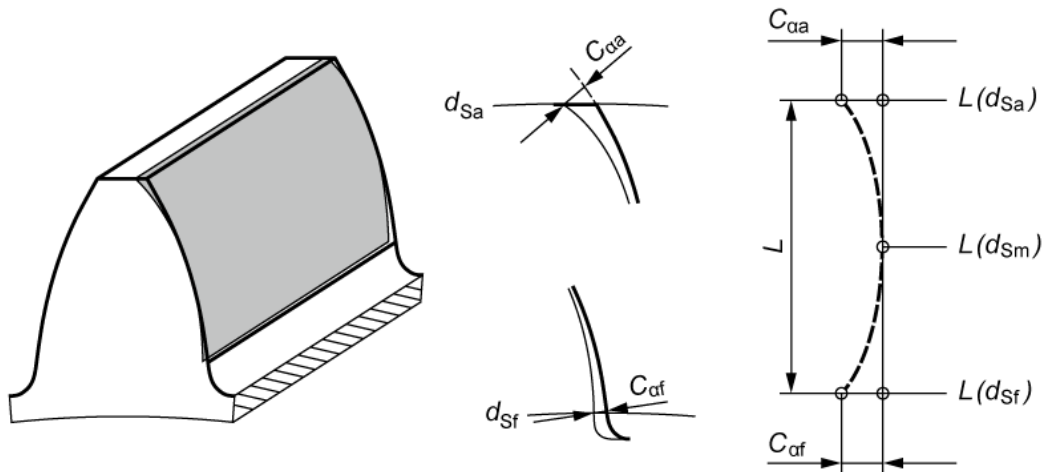


$d_{Sa}$	modification, start, at tip	$d_{Sr}$	modification, end, at root
$C_{aa}$	tip relief, value, normal to involute	$L_{Ca}$	tip relief, roll length
$C_{af}$	profile crowning, value	$L$	roll length

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{af}$	$L_{Ca}/m_n$	$1000 \cdot C_{aa}/m_n$
<b>Conditions</b>	$\neq 0$	$> 0$	$> 0$

## 1.6 Profile crowning (roll length-centered)

Picture: **Mod\_profileCrowning.png**



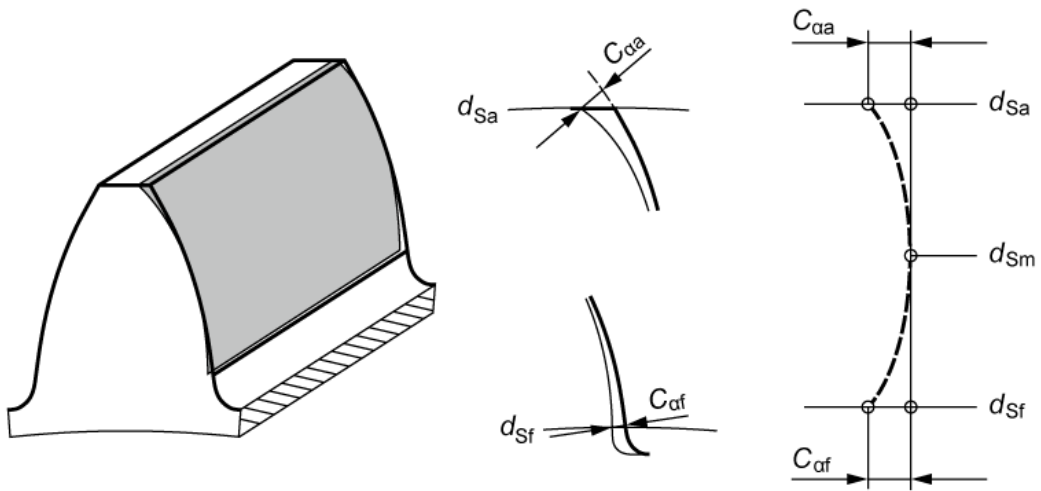
$d_{sa}$	profile crowning, start, at tip	$d_{sf}$	profile crowning, end, at root
$C_{aa}$	profile crowning, value, at tip, normal to involute	$C_{af}$	profile crowning, value, at root, normal to involute
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa} = C_{af}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	$L(d_{sm}) = 0.5 \cdot (L(d_{sa}) + L(d_{sf}))$		



## 1.7 Profile crowning (diameter-centered)

Picture: Mod\_profileCrowningDia.png

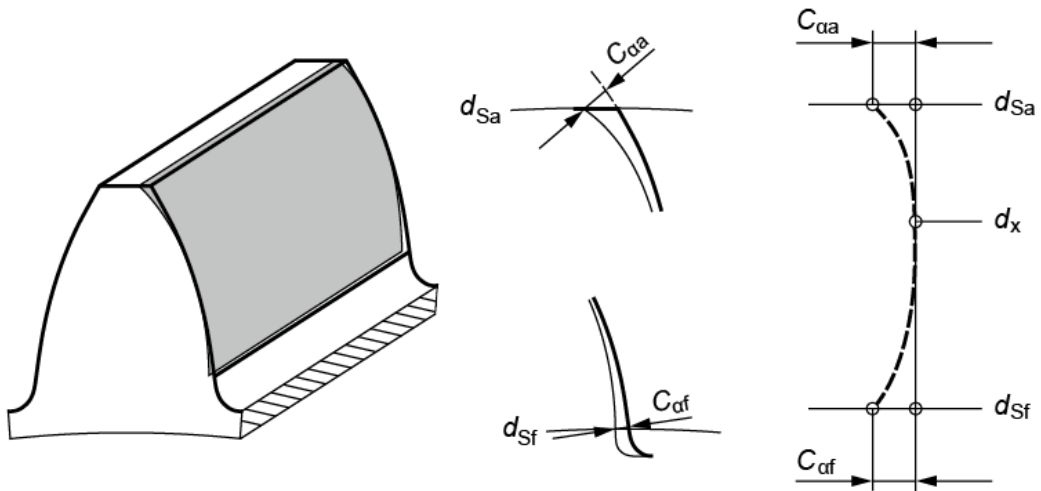


$d_{Sa}$	profile crowning, start, at tip	$d_{Sf}$	profile crowning, end, at root
$C_{aa}$	profile crowning, value, at tip, normal to involute	$C_{af}$	profile crowning, value, at root, normal to involute

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa} = C_{af}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	$d_{Sm} = 0.5 \cdot (d_{Sa} + d_{Sf})$		

## 1.8 Profile crowning, eccentric

Picture: **Mod\_profileCrowningExc.png**

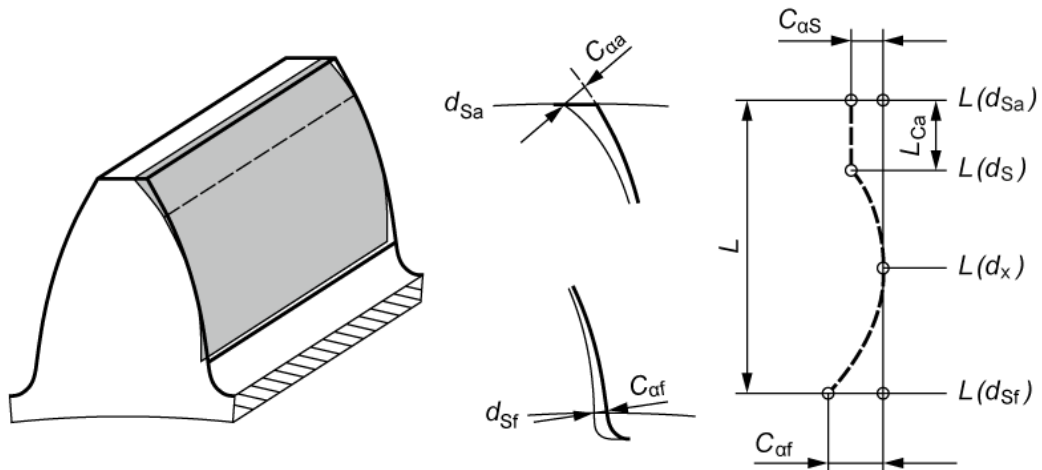


$d_{Sa}$	profile crowning, start, at tip	$d_{Sf}$	profile crowning, end, at root
$C_{aa}$	profile crowning, value, at tip, normal to involute	$C_{af}$	profile crowning, value, at root, normal to involute
$L_x$	tip to profile crowning vertex, roll length	$L$	roll length

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{aa}$	$(d_{Sa}-d_x)/(d_{Sa}-d_{Sf})$	$C_{af} / C_{aa}$
<b>Conditions</b>	$\neq 0$	$< 1$	$\geq 0$

## 1.9 Profile crowning, shortened

Picture: Mod\_profileCrowningShort.png

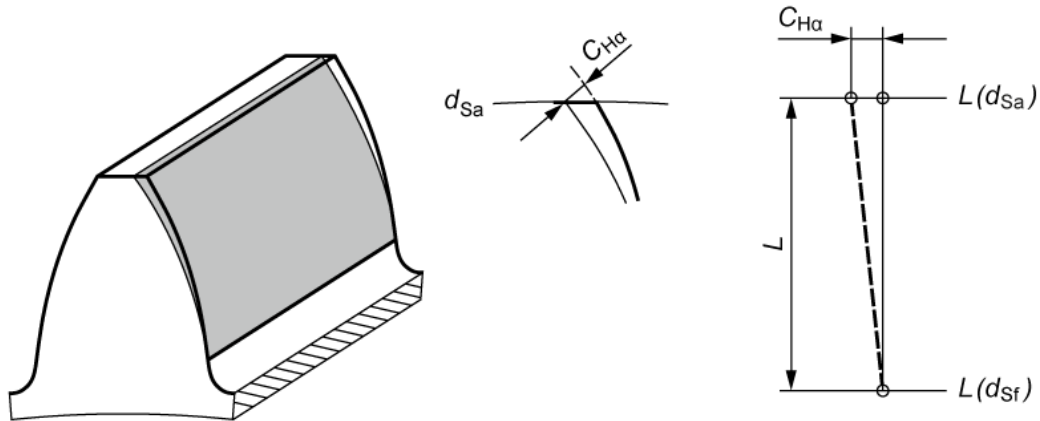


$d_{Sa}$	modification, start, at tip	$d_{Sf}$	modification, start, at root
$C_{Cf}$	profile crowning, value, at root, normal to involute	$L_{Ca}$	tip to profile crowning start, roll length
$L_x$	tip to profile crowning vertex, roll length	$L$	roll length

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{Cf}$	$(d_{Sa}-d_x)/(d_{Sa}-d_{Sf})$	$(d_{Sa}-d_S)/(d_{Sa}-d_{Sf})$
<b>Conditions</b>	$\neq 0$	$0 < \text{Factor 1} < 1$	$0 < \text{Factor 2} < 1$

## 1.10 Pressure angle modification (value), Transverse profile slope modification (value)

Picture: Mod\_pressureAngle.png

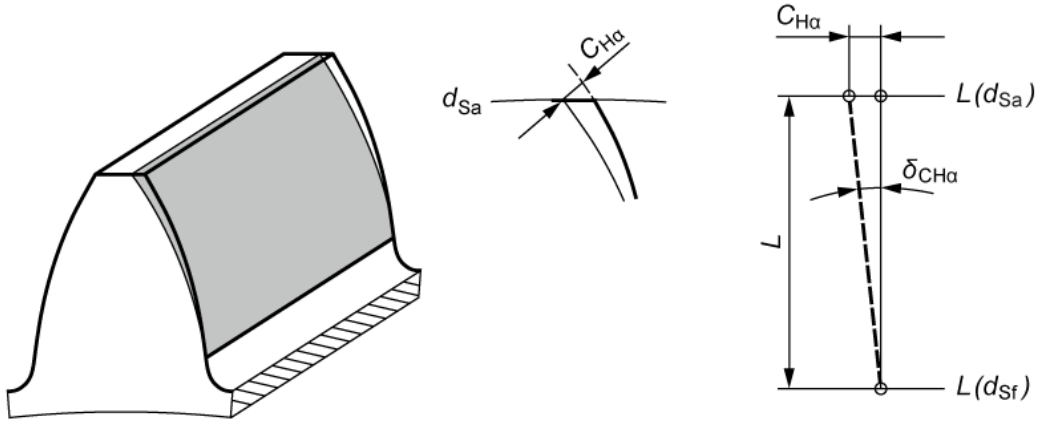


$d_{Sa}$	transverse profile slope modification, start, at tip	$d_{Sf}$	transverse profile slope modification, end, at root
$C_{Ha}$	transverse profile slope modification, value, normal to involute	$L$	roll length
$\alpha_{n\,eff}$	effective pressure angle		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{Ha}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	$\alpha_{n\,eff} = atan(\cos(\beta) \cdot \tan(\alpha_t + 0.001 \cdot C_{Ha} / Abs(L(d_{Sa}) - L(d_{Sf}))) / \tan \alpha_t)$		

## 1.11 Pressure angle modification (angle), Transverse profile slope modification (angle)

Picture: Mod\_pressureAngleAng.png

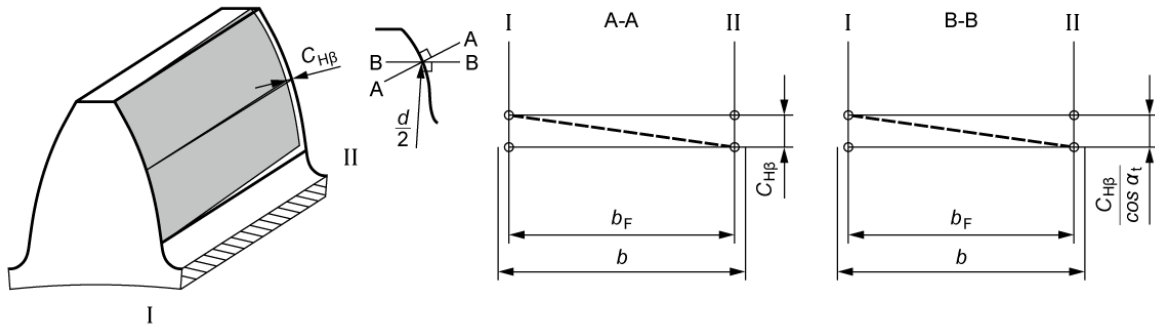


$d_{sa}$	transverse profile slope modification, start, at tip	$d_{sf}$	transverse profile slope modification, end, at root
$C_{H\alpha}$	transverse profile slope modification, value, normal to involute	$\delta_{CH\alpha}$	transverse profile slope modification, value, angle
$L$	roll length	$\alpha_{n\,eff}$	effective pressure angle

	Value	Factor 1	Factor 2
<b>Inputs</b>	-	$\delta_{CH\alpha}$ (in arc minutes)	-
<b>Conditions</b>	-	$\neq 0$	-
<b>Equation</b>	$C_{H\alpha} = 1000 \cdot \tan \alpha_t \cdot (\text{Factor } 1/60 / \cos \beta) \cdot \text{Abs}(L(d_{sa}) - L(d_{sf}))$ $\alpha_{n\,eff} = \text{atan}(\cos(\beta) \cdot \tan(\alpha_t + 0.001 \cdot C_{H\alpha} / \text{Abs}(L(d_{sa}) - L(d_{sf}))) / \tan \alpha_t)$		

# 1.12 Helix angle modification, tapered or conical

Picture: Mod\_helixAngleCon.png



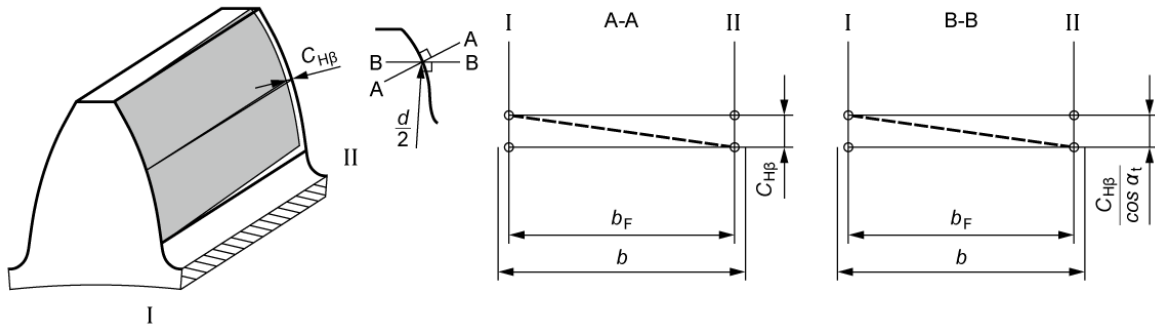
Spur	Right helix	Left helix

$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_k$ )
$C_{H\beta}$	helix angle modification, value	$\beta_{eff}$	effective helix angle

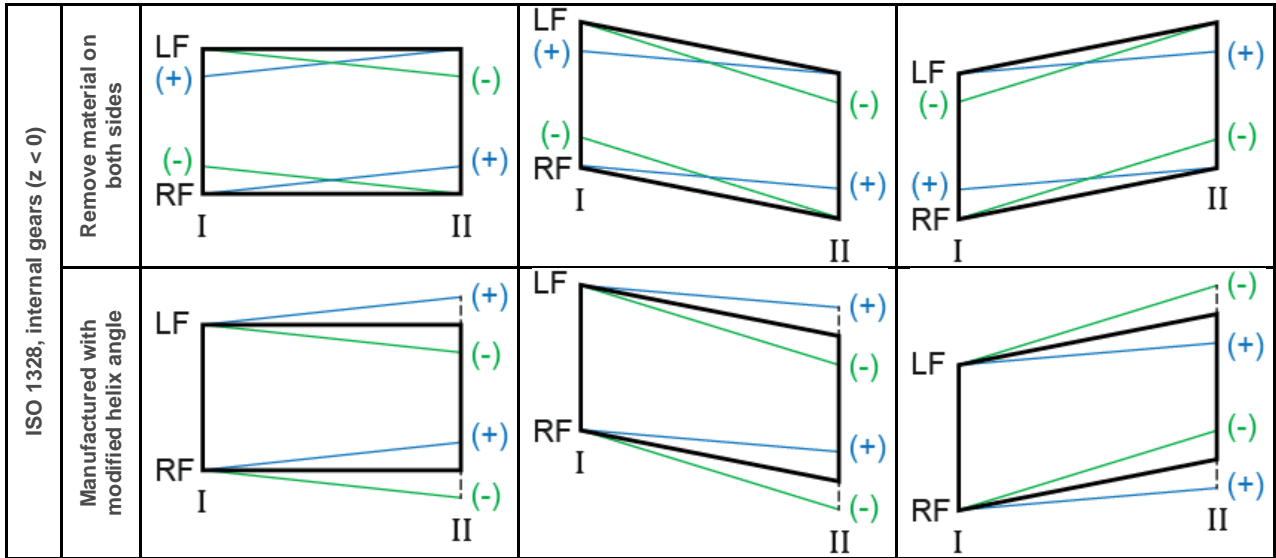
	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{H\beta}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	Equations apply only for individual flank. Helix angle of the gear is not affected. $C_{H\beta} = 1000 \cdot b_F \cdot \cos \alpha_t \cdot (\tan(\beta_{eff}) - \tan(\beta))$ $\beta_{eff} = \text{atan}((b_F \cdot \tan \beta \pm \text{Abs}(0.001 \cdot C_{H\beta} / \cos \alpha_t)) / b_F)$		

# 1.13 Helix angle modification, parallel (value)

Picture: Mod\_helixAngle.png



		Spur	Right helix	Left helix
ISO 21771	Remove material on both sides			
	Manufactured with modified helix angle			
ISO 1328, external gears (z > 0)	Remove material on both sides			
	Manufactured with modified helix angle			



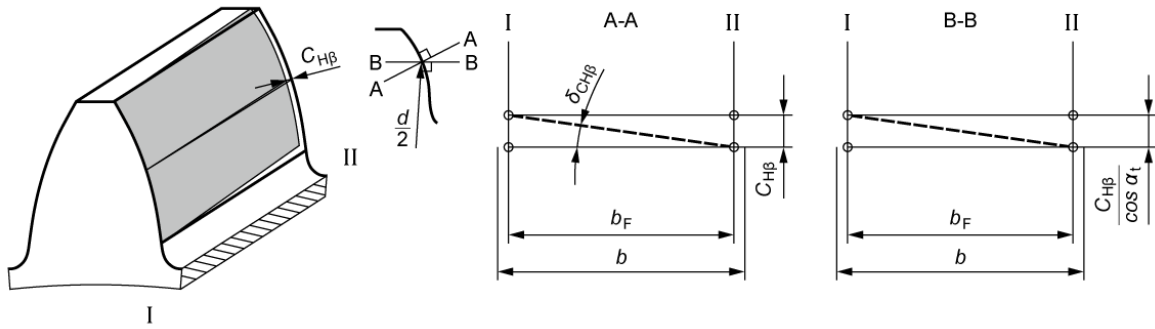
$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_k$ )
$C_{H\beta}$	helix angle modification, value	$\beta_{eff}$	effective helix angle

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{H\beta}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	$C_{H\beta} = 1000 \cdot \cos \alpha_n \cdot b_F \cdot (\tan(\beta - \text{Factor 1}/60) - \tan(\beta))$ $\beta_{eff} = \text{atan}((b_F \cdot \tan \beta \pm \text{Abs}(0.001 \cdot C_{H\beta} / \cos \alpha_i)) / b_F)$ More information in Instruction 117: Definition of helix angle modification		

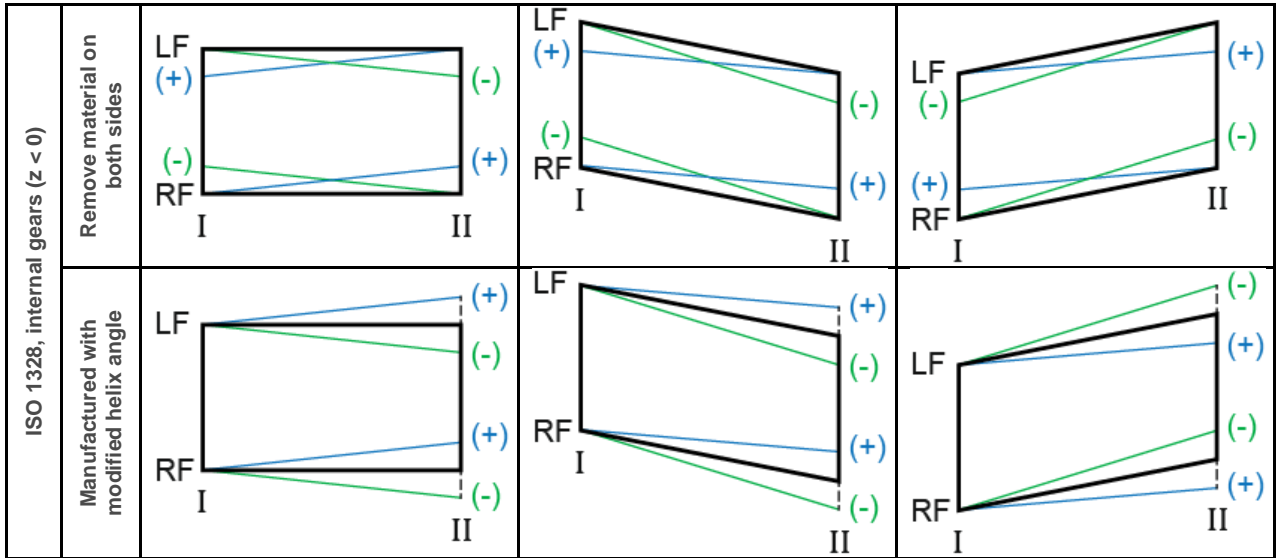


# 1.14 Helix angle modification, parallel (angle)

Picture: Mod\_helixAngleAng.png



		Spur	Right helix	Left helix
ISO 21771	Remove material on both sides			
	Manufactured with modified helix angle			
ISO 1328, external gears (z > 0)	Remove material on both sides			
	Manufactured with modified helix angle			

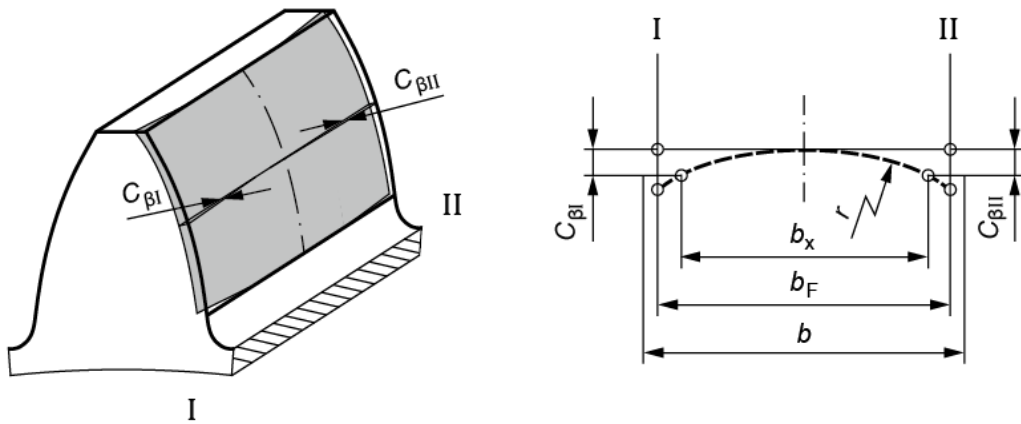


$b$	facewidth	$b_F$	usable facewidth ( $b-2 \cdot b_K$ )
$C_{H\beta}$	helix angle modification, value	$\delta_{CH\beta}$	helix angle modification, value, angle
$\beta_{eff}$	effective helix angle		

	Value	Factor 1	Factor 2
Inputs	-	$\delta_{CH\beta}$ (in arc minutes)	-
Conditions	-	$\neq 0$	-
Equation	$\beta_{eff} = \text{atan} \left( \frac{b_F \cdot \tan \beta \pm \text{Abs}(0.001 \cdot C_{H\beta} / \cos \alpha_t)}{b_F} \right)$ More information in Instruction 117: Definition of helix angle modification		

## 1.15 Flank line crowning

Picture: **Mod\_flankCrowning.png**

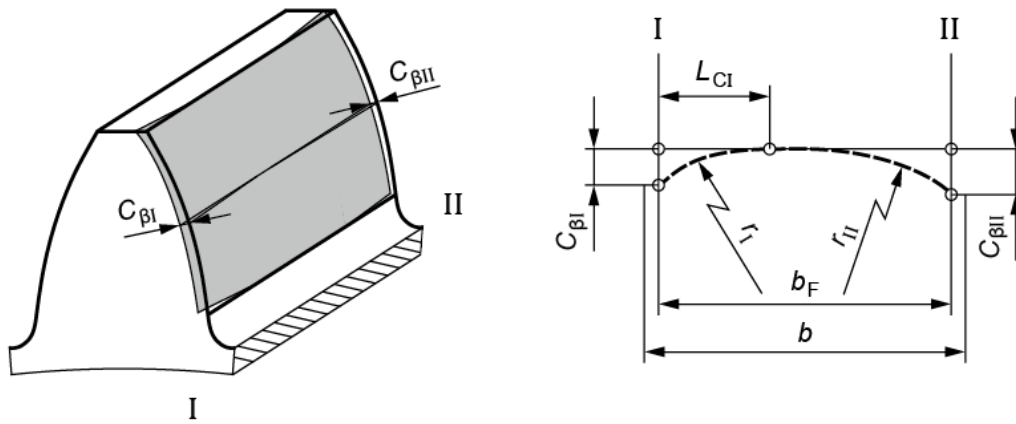


$b$	facewidth	$b_F$	usable facewidth ( $b-2 \cdot b_R$ )
$b_x$	reference width	$C_{\beta I}$	flank line crowning, value, at side I
$C_{\beta II}$	flank line crowning, value, at side II	$r$	flank line crowning, radius

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{\beta I} = C_{\beta II}$	$b_x/b_F$	-
<b>Conditions</b>	$\neq 0$	$0 < \text{Factor 1} \leq 1$	-

## 1.16 Flank line crowning, eccentric

Picture: **Mod\_flankCrowningExc.png**

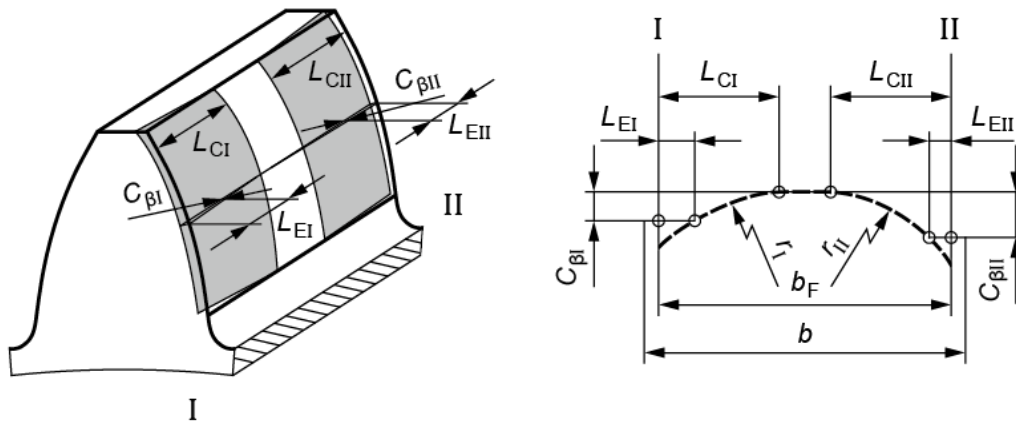


$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_K$ )
$C_{\beta I}$	flank line crowning, value, at side I	$C_{\beta II}$	flank line crowning, value, at side II
$r_I$	flank line crowning, radius, at side I	$r_{II}$	flank line crowning, radius, at side II
$L_{CI}$	side I to crowning vertex, length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{\beta I}$	$L_{CI}/b_F$	$C_{\beta II}/C_{\beta I}$
<b>Conditions</b>	$\neq 0$	$0 < \text{Factor 1} < 1$	$> 0$

## 1.17 Flank line crowning, side I and II

Picture: **Mod\_flankCrowningShort.png**

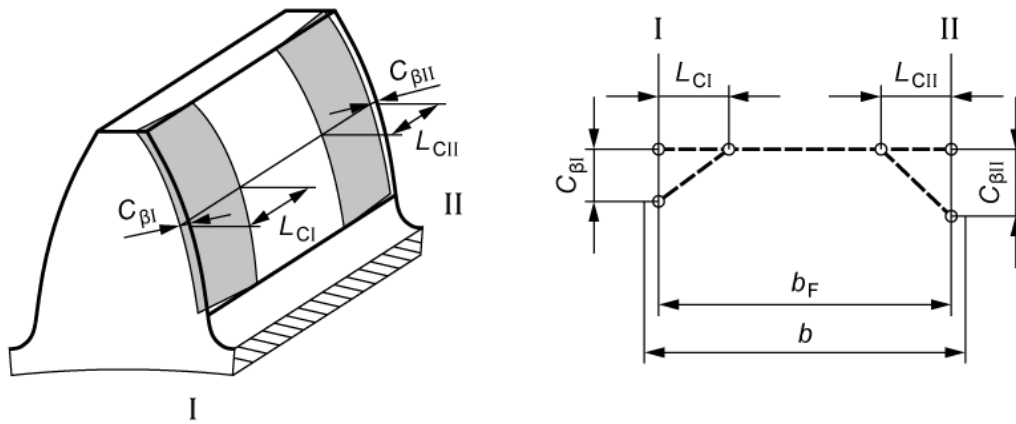


$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_R$ )
$C_{\beta I}$	flank line crowning, value, at $L_{EI}$ , at side I	$C_{\beta II}$	flank line crowning, value, at $L_{EII}$ , at side II
$r_I$	flank line crowning, radius, at side I	$r_{II}$	flank line crowning, radius, at side II
$L_{CI}$	flank line crowning, length, at side I	$L_{CII}$	flank line crowning, length, at side II

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{\beta I}, C_{\beta II}$	$L_{CI}/b_F, L_{CII}/b_F$	$L_{EI}/b_F, L_{EII}/b_F$
<b>Conditions</b>	$> 0$	$Factor\ 2 < Factor\ 1 < 1$	$0 < Factor\ 2 < Factor\ 1$

## 1.18 End relief, linear, side I and II

Picture: Mod\_endRelief.png

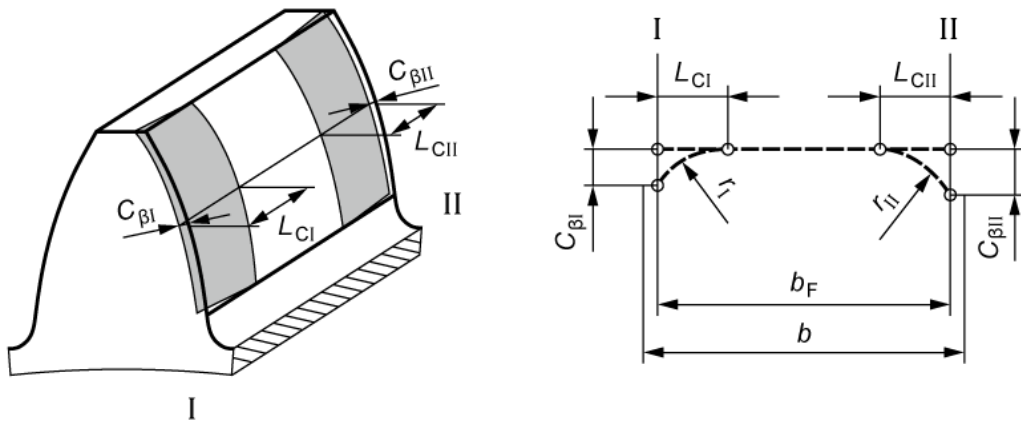


$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_R$ )
$C_{\beta I}$	end relief, value, at side I	$C_{\beta II}$	end relief, value, at side II
$L_{C I}$	end relief, length, at side I	$L_{C II}$	end relief, length, at side II

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{\beta I}, C_{\beta II}$	$L_{C I}/b_F, L_{C II}/b_F$	-
<b>Conditions</b>	$> 0$	$0 < \text{Factor 1} < 1$	-

## 1.19 End relief, arc-like, side I and II

Picture: Mod\_endReliefArc.png

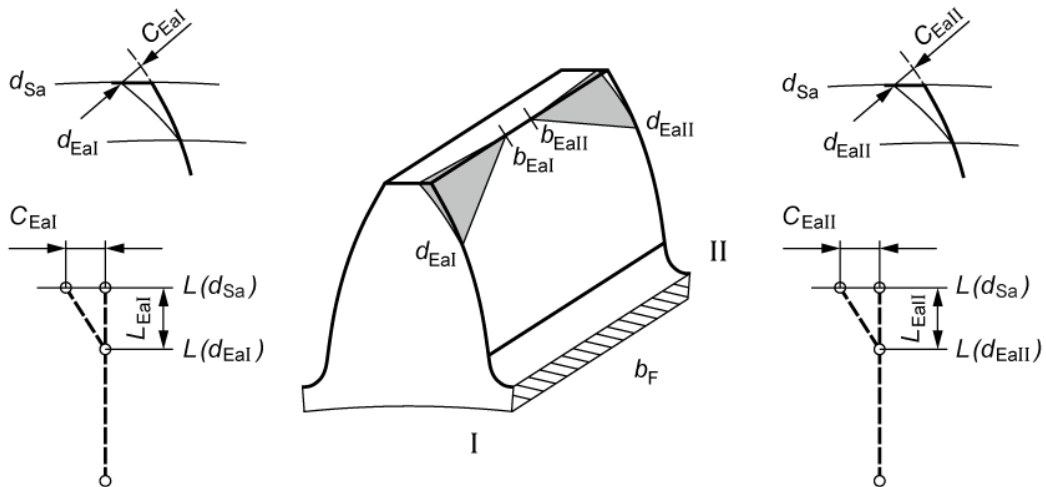


$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_k$ )
$C_{\beta I}$	end relief, value, at side I	$C_{\beta II}$	end relief, value, at side II
$r_I$	end relief, radius, at side I	$r_{II}$	end relief, radius, at side II
$L_{cI}$	end relief, length, at side I	$L_{cII}$	end relief, length, at side II

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{\beta I}, C_{\beta II}$	$L_{cI}/b_F, L_{cII}/b_F$	-
<b>Conditions</b>	$> 0$	$0 < \text{Factor 1} < 1$	-

## 1.20 Triangular end relief, side I and II

Picture: **Mod\_triangularRelief.png**



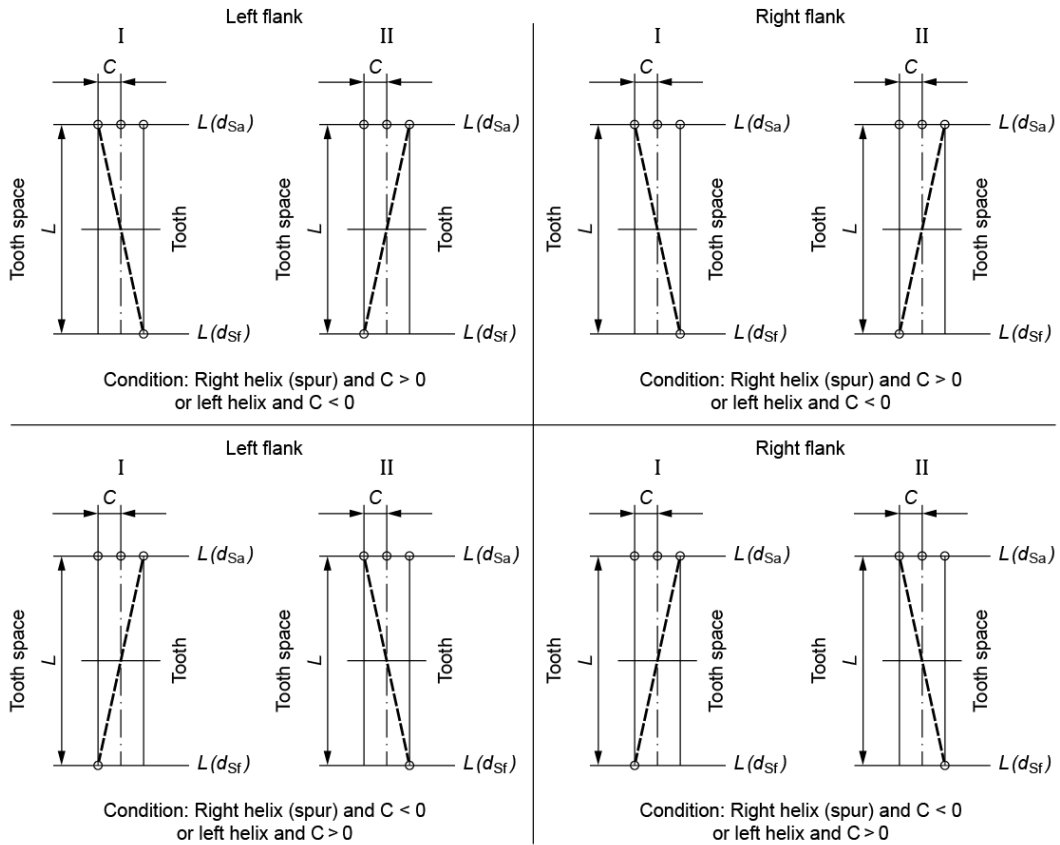
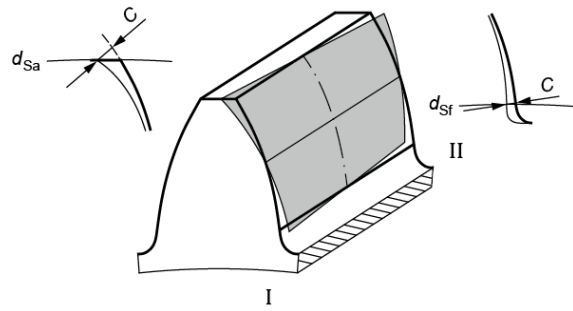
$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_K$ )
$d_{Sa}$	triangular relief, start, at side I	$d_{Sa}$	triangular relief, start, at side II
$d_{Eal}$	triangular relief, end, at side I	$d_{Eall}$	triangular relief, end, at side II
$C_{Eal}$	triangular relief, value, at side I	$C_{Eall}$	triangular relief, value, at side II
$b_{Eal}$	triangular relief, length, at side I	$b_{Eall}$	triangular relief, length, at side II

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_{Eal}, C_{Eall}$	$L_{Eal}/m_n, L_{Eall}/m_n$	$b_{Eal}/b_F, b_{Eall}/b_F$
<b>Conditions</b>	$> 0$	$> 0$	$0 < \text{Factor 2} < 1$



# 1.21 Twist

Picture: Mod\_twist.png

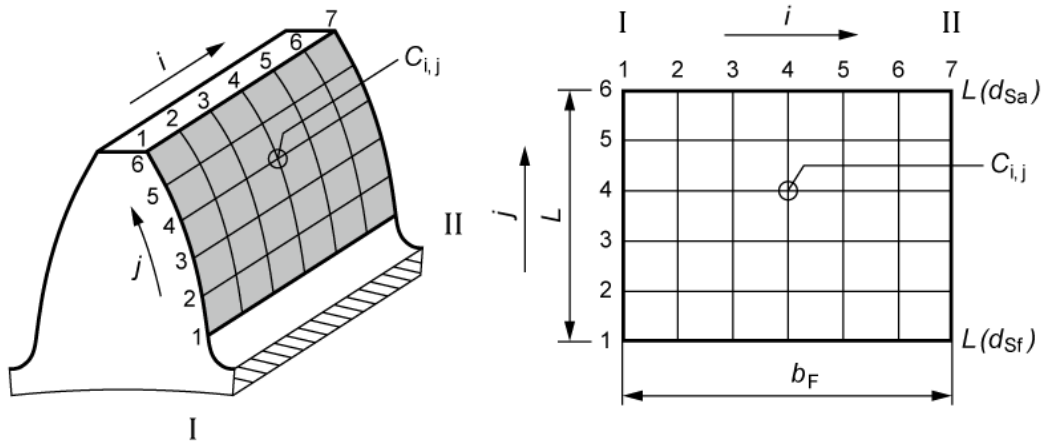


$d_{Sa}$	twist, start, at tip	$d_{Sf}$	twist, end, at root
$C$	twist, value		

	Value	Factor 1	Factor 2
Inputs	$4 \cdot C$	-	-
Conditions	$\neq 0$	-	-

## 1.22 Topological modification

Picture: **Mod\_topological.png**



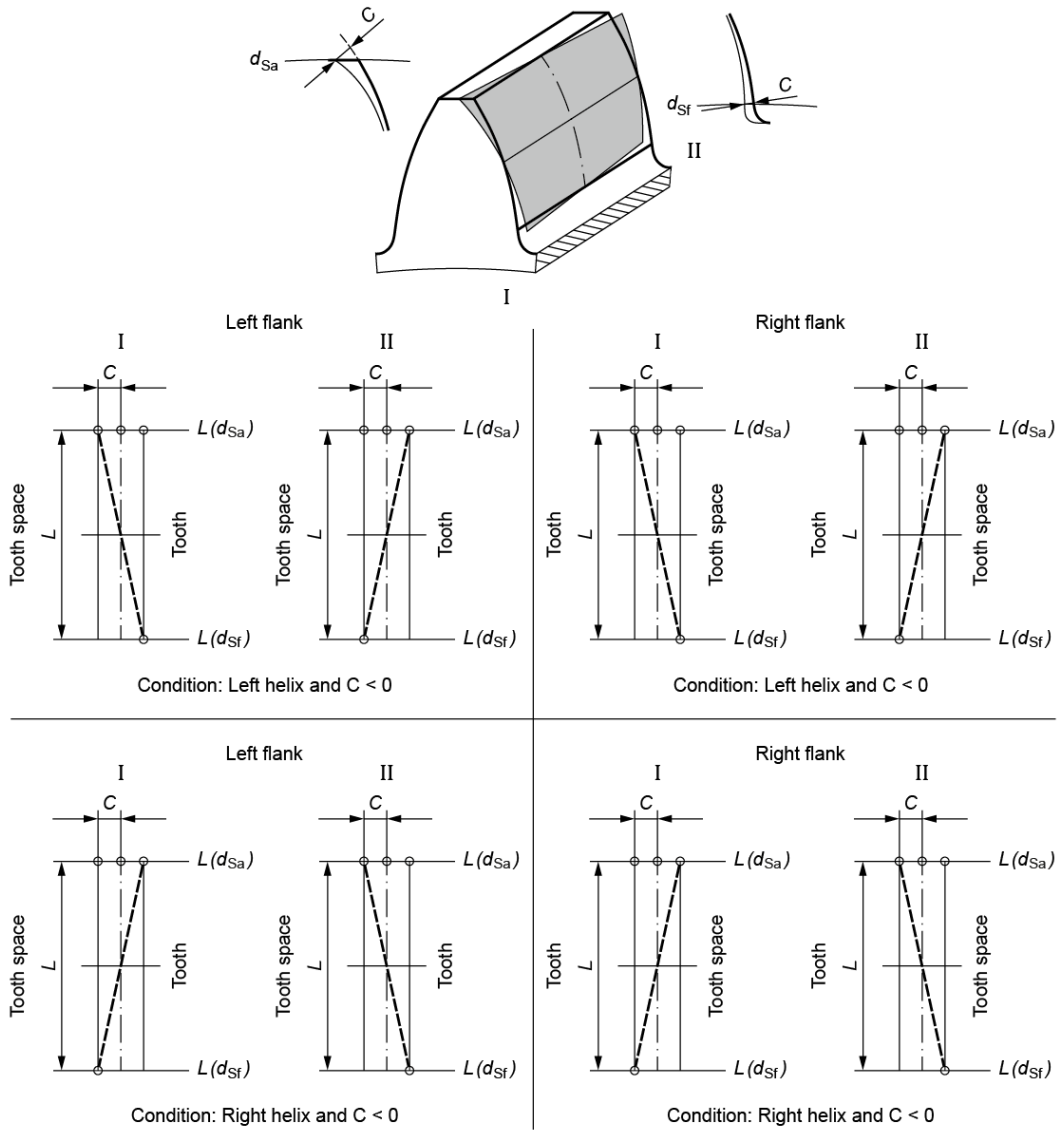
$d_{sa}$	topological modification, start, at tip	$d_{sf}$	topological modification, end, at root
$b_F$	usable facewidth ( $b-2 \cdot b_k$ )	$C_{i,j}$	topological modification, value, at position $i,j$
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	see manual	-	-
<b>Conditions</b>	$> 0$	-	-

## 2 Manufacturing deviations

### 2.1 Natural twist from flank line crowning $C_\beta$ (generation grinding)

Picture: Mod\_twistManufacturing.png

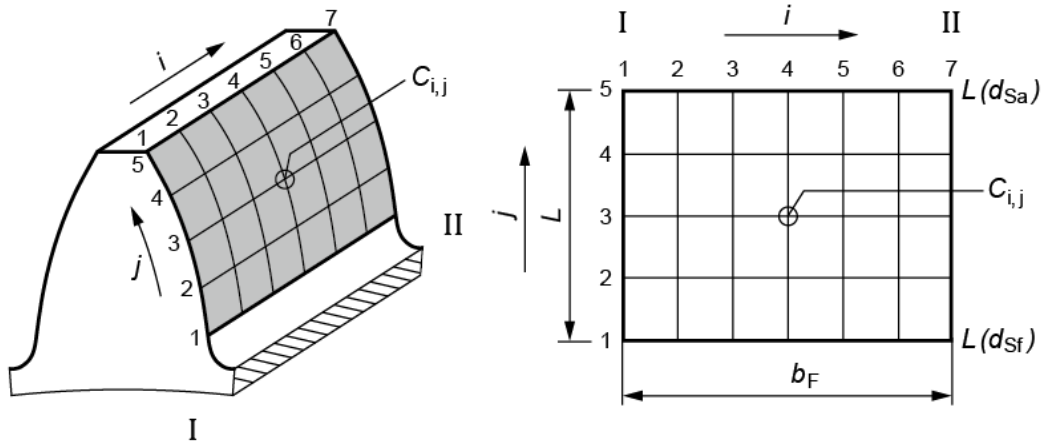


$d_{Sa}$	natural twist, start, at tip	$d_{Sf}$	natural twist, end, at root
$C$	natural twist, value, $f(C_\beta)$	$C_\beta$	flank line crowning

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C_\beta$ , see manual	-	-
<b>Conditions</b>	$> 0$	-	-
<b>Info</b>	Natural twist value $C$ is always negative.		

## 2.2 Measured manufacturing deviation

Picture: Mod\_topological.png



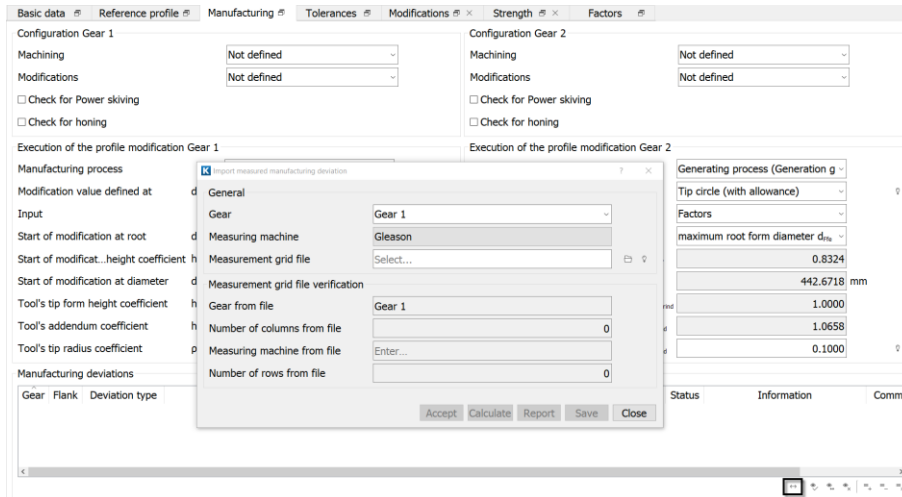
$d_{sa}$	measured manufacturing deviation, start, at tip	$d_{sf}$	measured manufacturing deviation, end, at root
$b_F$	usable facewidth ( $b-2 \cdot b_k$ )	$C_{i,j}$	measured manufacturing deviation, value, at position $i,j$
$L$	roll length		

	Value	Factor 1	Factor 2
<b>Inputs</b>	see manual	-	-
<b>Conditions</b>	$> 0$	-	-

The measured manufacturing deviation option enables you to import the Gleason GAMA CMM data directly and converted into the topological modification format used in KISSsoft. Thus, the format of the template for the measured manufacturing deviation modification is the same as the topological modification template. It is assumed the values in the template are defined in  $\mu\text{m}$ . To display the modification, select Graphics > 3D Geometry > Modifications.

By defining the modification, the user can analyze the effect of the manufacturing deviation on gear performances such as transmission error, contact stress, and other characteristics. This function is essential in the "Design – Manufacturing – Measuring Closed Loop" to ensure the manufactured gears perform desired characteristics.

It is possible to define the modification manually, but it is recommended to use the "Import measured manufacturing deviation" conversion dialogue in the Manufacturing tab.



The user should assign the CMM data that contains manufacturing deviation in the window. Currently, only the Gleason GAMA data format is allowed. Note that it should contain the deviation data shown under the column FN.

```

*****
*                                     MEASUREMENT DATA - LIST
*                                     PINION CONVEX
*-----*
*DRAWING NUMBER :
*ANGULAR TOOTH-THICKNESS ERROR % ZDIF !-16.2653 [DEG] % (J,I) ! (5,3)
*-----*
*COLUMNS % NSPG ! 9 ; LINES % NZLG ! 5
*-----*
*DATE : 15 Jun 2020
*****
*   J   I       XP       YP       ZP                                     FN
*23456789012345678901234567890123456789012345678901234567890123456789*
  1   1       15.2990    -2.7665    -9.3186                                     -.00691
  1   2       16.2254    -3.4014    -9.3189                                     -.00569
  1   3       17.0949    -4.2238    -9.3188                                     -.00589
  1   4       17.8968    -5.2083    -9.3186                                     -.00722
  1   5       18.6213    -6.3386    -9.3186                                     -.00699
  2   1       15.4391    -1.8344    -6.9890                                     -.00496
  2   2       16.4024    -2.4126    -6.9892                                     -.00422
  2   3       17.3205    -3.1807    -6.9892                                     -.00384
  2   4       18.1808    -4.1149    -6.9890                                     -.00501
  2   5       19.0900    -5.1000    -6.9890                                     -.00500
  3   1       15.4391    -1.8344    -6.9890                                     -.00496
  3   2       16.4024    -2.4126    -6.9892                                     -.00422
  3   3       17.3205    -3.1807    -6.9892                                     -.00384
  3   4       18.1808    -4.1149    -6.9890                                     -.00501
  3   5       19.0900    -5.1000    -6.9890                                     -.00500
  4   1       15.4391    -1.8344    -6.9890                                     -.00496
  4   2       16.4024    -2.4126    -6.9892                                     -.00422
  4   3       17.3205    -3.1807    -6.9892                                     -.00384
  4   4       18.1808    -4.1149    -6.9890                                     -.00501
  4   5       19.0900    -5.1000    -6.9890                                     -.00500
  5   1       15.4391    -1.8344    -6.9890                                     -.00496
  5   2       16.4024    -2.4126    -6.9892                                     -.00422
  5   3       17.3205    -3.1807    -6.9892                                     -.00384
  5   4       18.1808    -4.1149    -6.9890                                     -.00501
  5   5       19.0900    -5.1000    -6.9890                                     -.00500
*****

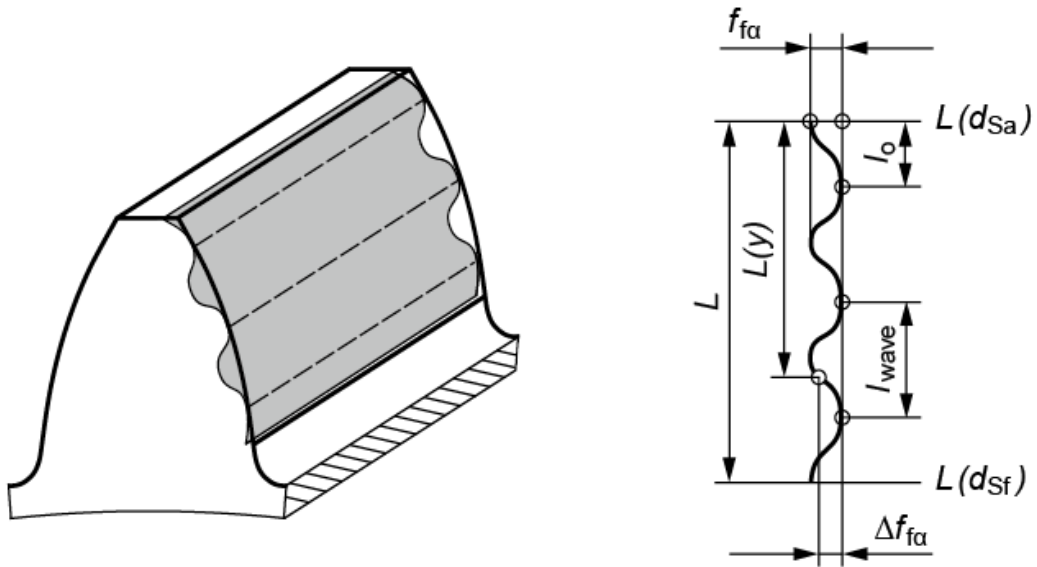
```

After assigned the file, click “Calculate” and “Save” button to save the template files into proper folder. After saving the file, click “Accept” button, and the program will create the entry of the modifications automatically as shown below.

Gear	Flank	Deviation type	Value [µm]	Data file	Status	Information
Gear 1	both	Measured manufacturing deviation		template.dat	active	?
Gear 2	both	Measured manufacturing deviation		template.dat	active	?

### 2.3 Profile form deviation $f_{f\alpha}$

Picture: Mod\_formErrorfFa.png

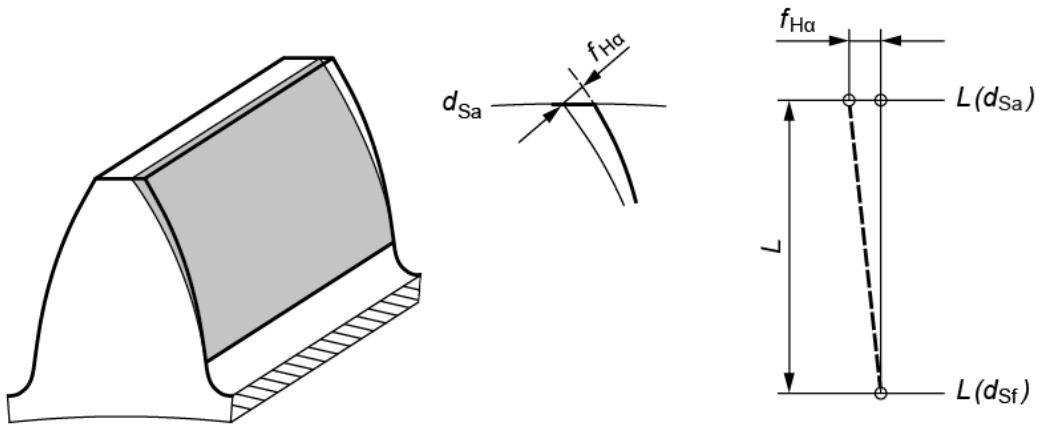


$d_{Sa}$	profile form deviation, start, at tip	$d_{Sf}$	profile form deviation, end, at root
$L$	roll length	$l_o$	phase shift
$l_{wave}$	wave length	$f_{f\alpha}$	profile form deviation, value

	Value	Factor 1	Factor 2
<b>Inputs</b>	$f_{f\alpha}$	$l_{wave}/m_n$	$l_o/m_n$
<b>Conditions</b>	$> 0$	$> 0$	-
<b>Equation</b>	$\Delta f_{f\alpha} = \frac{f_{f\alpha}}{2} \cdot \left[ 1 - \sin \left( 90^\circ + 360^\circ \cdot \left( \frac{L(y)}{Factor\ 1 \cdot m_n} - \frac{Factor\ 2}{Factor\ 1} \right) \right) \right]$		

## 2.4 Profile slope deviation $f_{H\alpha}$

Picture: **Mod\_formErrorfHa.png**

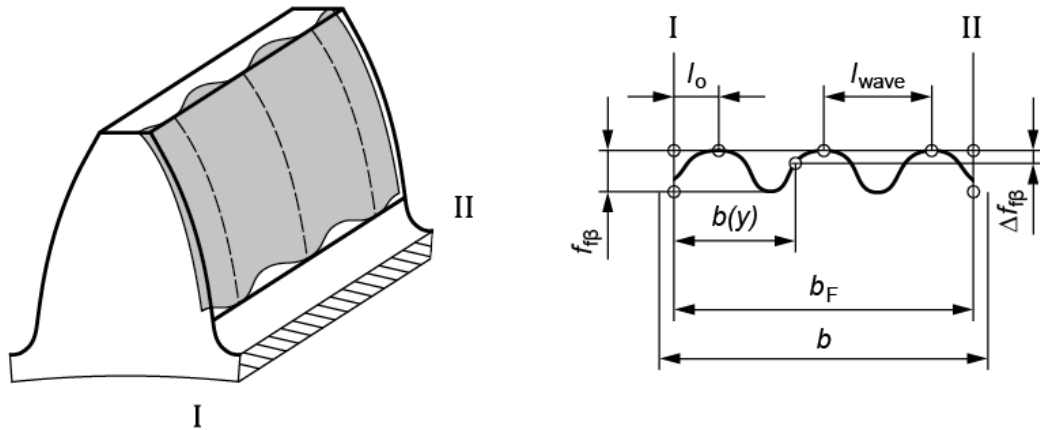


$d_{Sa}$	profile slope deviation, start, at tip	$d_{Sf}$	profile slope deviation, end, at root
$f_{H\alpha}$	profile slope deviation, value, normal to involute	$L$	roll length

	Value	Factor 1	Factor 2
<b>Inputs</b>	$f_{H\alpha}$	-	-
<b>Conditions</b>	$\neq 0$	-	-

## 2.5 Helix form deviation $f_{f\beta}$

Picture: **Mod\_formErrorfFb.png**



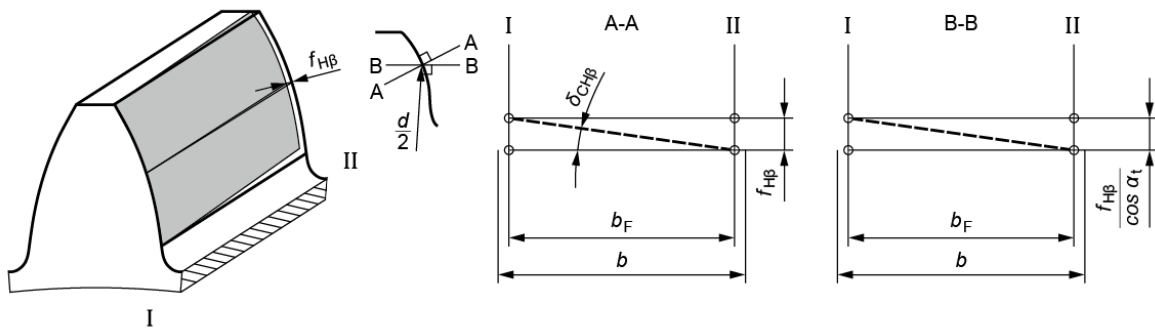
$b$	facewidth	$b_F$	usable facewidth ( $b-2 \cdot b_k$ )
$l_o$	phase shift	$l_{wave}$	wave length
$f_{f\beta}$	helix form deviation, value		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$f_{f\beta}$	$l_{wave}/m_n$	$l_o/m_n$
<b>Conditions</b>	$> 0$	$> 0$	-
<b>Equation</b>	$\Delta f_{f\beta} = \frac{f_{f\beta}}{2} \cdot \left[ 1 - \sin \left( 90^\circ + 360^\circ \cdot \left( \frac{b(y)}{Factor\ 1 \cdot m_n} - \frac{Factor\ 2}{Factor\ 1} \right) \right) \right]$		

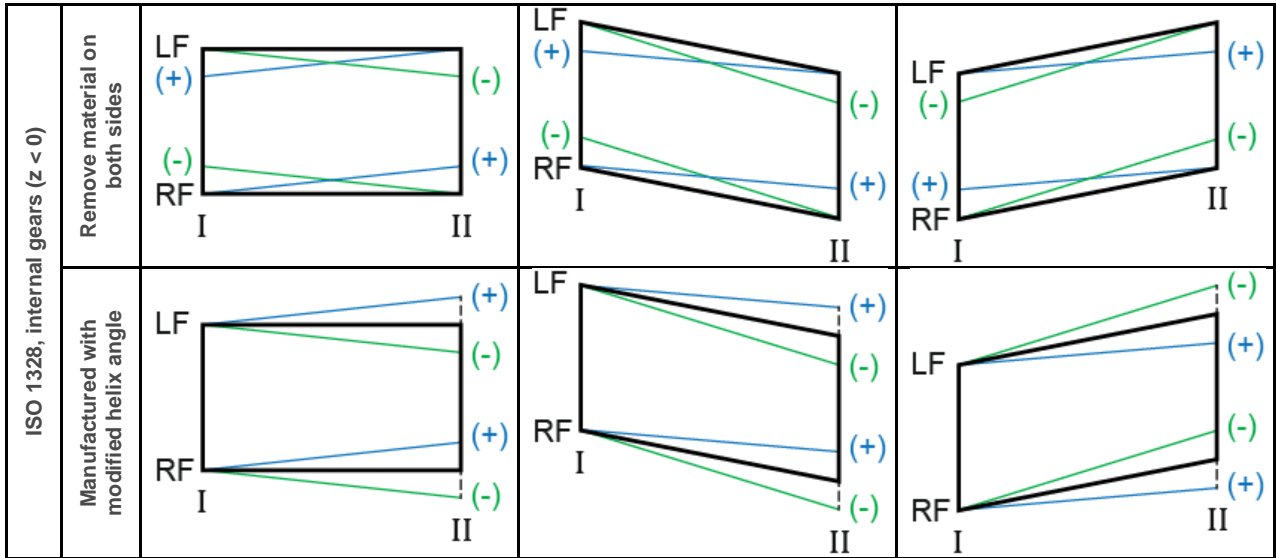


## 2.6 Helix slope deviation $f_{H\beta}$

Picture: **Mod\_formErrorfHb.png**



		Spur	Right helix	Left helix
ISO 21771	Remove material on both sides			
	Manufactured with modified helix angle			
ISO 1328, external gears ( $z > 0$ )	Remove material on both sides			
	Manufactured with modified helix angle			

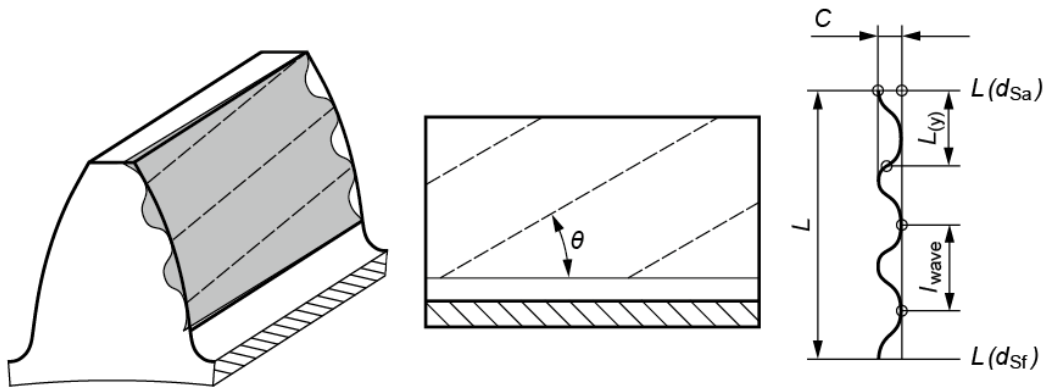


$b$	facewidth	$b_F$	usable facewidth ( $b - 2 \cdot b_k$ )
$f_{H\beta}$	helix slope deviation, value		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$f_{H\beta}$	-	-
<b>Conditions</b>	$\neq 0$	-	-
<b>Equation</b>	$f_{H\beta} = 1000 \cdot \cos \alpha_n \cdot b_F \cdot (\tan(\beta - \text{Factor 1}/60) - \tan(\beta))$		

## 2.7 Waviness from manufacturing

Picture: **Mod\_cuttingError.png**



$d_{sa}$	waviness from manufacturing, start, at tip	$d_{sf}$	waviness from manufacturing, end, at root
$L$	roll length	$l_{wave}$	wave length
$C$	waviness from manufacturing, value		

	Value	Factor 1	Factor 2
<b>Inputs</b>	$C$	Factor 1	Factor 2 ( $^{\circ}$ )
<b>Conditions</b>	$> 0$	$> 0$	$> 0$
<b>Equation</b>	$l_{wave} = \text{Factor 1} \cdot m_n \cdot \cos(\text{Factor 2})$ $\Delta C = \frac{C}{2} \cdot \left[ 1 - \sin \left( 180^{\circ} + 360^{\circ} \cdot \left( \frac{L(y)}{l_{wave}} \right) \right) \right]$ <p>If Factor 2 = 0, the waviness is applied in the direction of the base helix angle <math>\beta_b</math>.</p>		