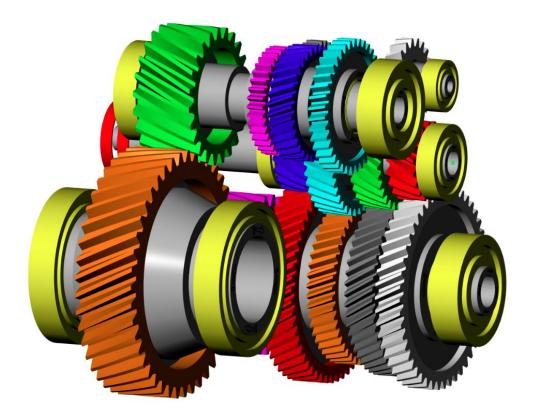
Efficient layout procedure of cylindrical gears with manufacturing constraints

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Introduction: calculation methods

Cylindrical gear strength can be calculation according to different standards:

ISO 6336, DIN 3990, AGMA 2001, AGMA 2101, VDI 2736, GOST 21354-87...

The main idea is to compare permissible values with calculated values:

$$Safety factor (Pitting) = \frac{permissible Stress}{calculated Stress}$$

$$Safety \ factor \ (Bending) = \frac{permissible \ Stress}{calculated \ Stress}$$

$$Safety\ factor\ (Scuffing) = \frac{permissible\ scuffing\ Temperature}{calculated\ contact\ Temperature}$$

$$Safety\ factor\ (Micropitting) = \frac{calculated\ minimum\ lubricant\ film\ Thickness}{permissible\ lubricant\ film\ Thickness}$$

The following condition has to hold:

$$S \geq S_{min}$$



Condition:

calculated contact stress ≤ permissible contact stress

$$\sigma_{H} \leq \sigma_{HP}$$

$$\begin{split} \sigma_{H} &= Z_{\mathcal{B}} \cdot \sigma_{HO} \cdot \sqrt{K_{\mathcal{A}} \cdot K_{\mathcal{V}} \cdot K_{H\beta} \cdot K_{H\alpha}} \leq \sigma_{HP} \\ \sigma_{HO} &= Z_{\mathcal{H}} \cdot Z_{\mathcal{E}} \cdot Z_{\mathcal{E}} \cdot Z_{\beta} \cdot \sqrt{\frac{F_{t}}{d_{1} \cdot b} \cdot \frac{u+1}{u}} \end{split}$$

$$\sigma_{HP} = \frac{\sigma_{H \text{ lim}} \cdot Z_{NT}}{S_{H \text{ min}}} \cdot Z_L \cdot Z_V \cdot Z_R \cdot Z_W \cdot Z_X = \frac{\sigma_{HG}}{S_{H \text{ min}}}$$





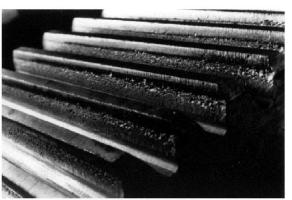
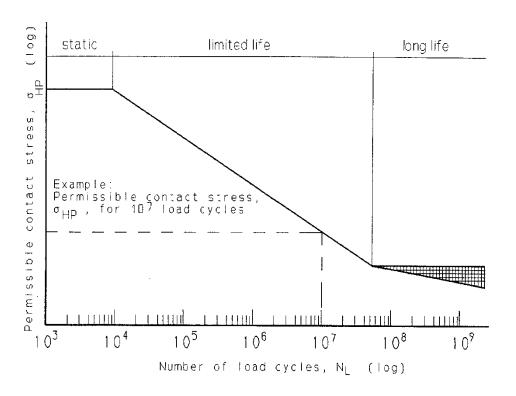


Figure 30 - Progressive pitting



Introduction: permissible contact stress (ISO 6336)



$$\sigma_{HP} = \frac{\sigma_{H \text{ lim}} \cdot Z_{NT}}{S_{H \text{ min}}} \cdot Z_L \cdot Z_V \cdot Z_R \cdot Z_W \cdot Z_X = \frac{\sigma_{HG}}{S_{H \text{ min}}}$$



Condition:

calculated root stress ≤ permissible root stress

$$\sigma_{F} \leq \sigma_{FP}$$

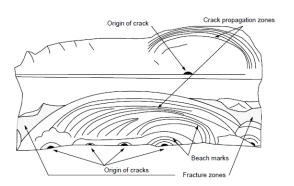
$$\sigma_F = \sigma_{FO} \cdot K_A \cdot K_V \cdot K_{F\beta} \cdot K_{F\alpha}$$

$$\sigma_{FP} = \frac{\sigma_{F \, \text{lim}} \cdot Y_{ST} \cdot Y_{NT}}{S_{F \, \text{min}}} \cdot Y_{\delta relT} \cdot Y_{RrelT} \cdot Y_{X} = \frac{\sigma_{FG}}{S_{F \, \text{min}}}$$

$$\sigma_{FO-B} = \frac{F_t}{b \cdot m_n} \cdot Y_F \cdot Y_S \cdot Y_\beta \cdot Y_B \cdot Y_{DT}$$

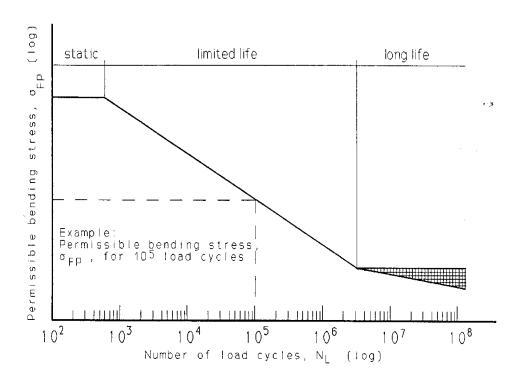


Figure 43 - Bending fatigue crack



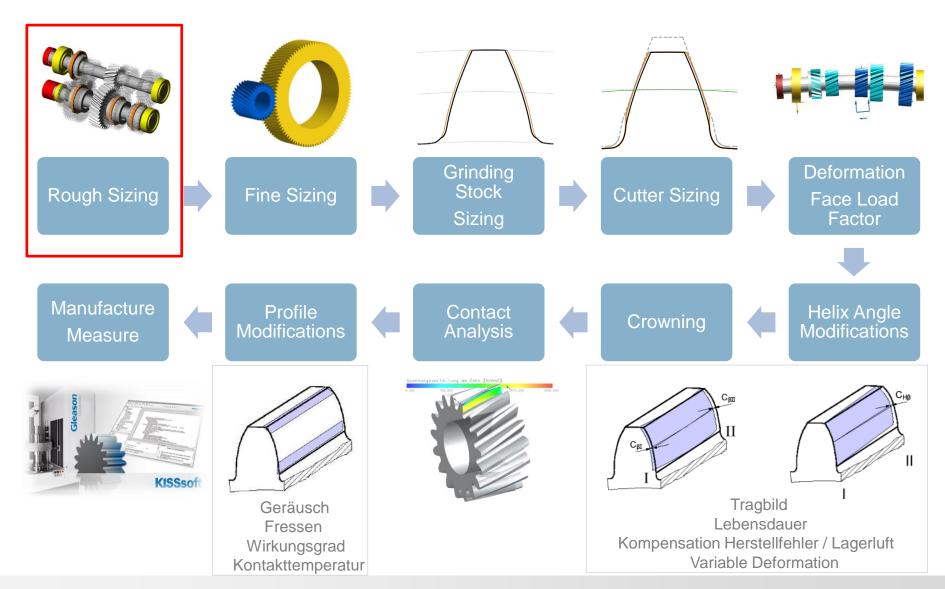


Introduction: permissible root stress (ISO 6336)

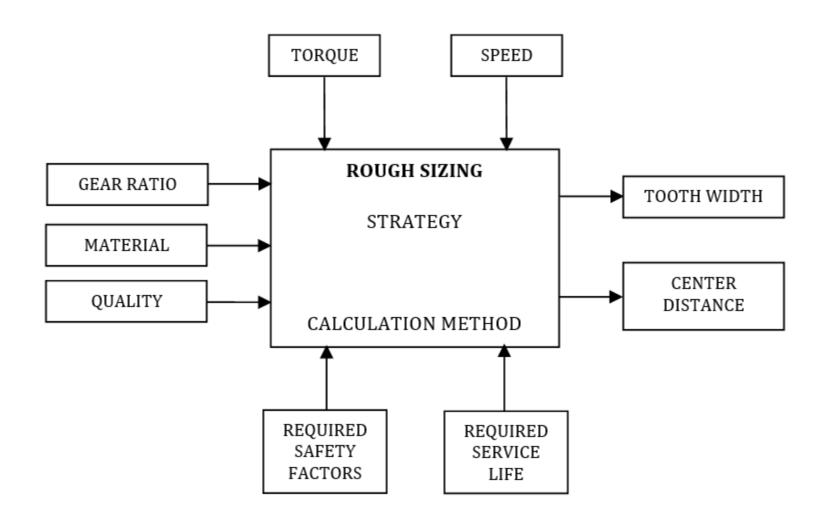


$$\sigma_{\mathit{FP}} = \frac{\sigma_{\mathit{F}\,\text{lim}} \cdot Y_{\mathit{ST}} \cdot Y_{\mathit{NT}}}{S_{\mathit{F}\,\text{min}}} \cdot Y_{\mathit{\delta relT}} \cdot Y_{\mathit{RrelT}} \cdot Y_{\mathit{X}} = \frac{\sigma_{\mathit{FG}}}{S_{\mathit{F}\,\text{min}}}$$











Goal: find optimal **center distance** and **face width**. This will define the gearbox dimensions.

The choice of optimal solution depends on the defined target(s):

- Low weight
- Low size
- Max. Torque
- Max. Power density

| a [mm] | b ₁ [mm] | b ₂ [mm] | m _n [mm] | Z ₁ | Z ₂ | İ | SF _{smallest} | SH _{smallest} | P _{max} [kW] | W [kg] | T _{max} /W [Nm/kg] | dB(A) |
|---------|---------------------|---------------------|---------------------|----------------|----------------|-------|------------------------|------------------------|-----------------------|--------|-----------------------------|--------|
| 97.660 | 60.930 | 59.440 | 2.972 | 16 | 49 | 3.063 | 2.330 | 1.000 | 49.952 | 8.547 | 37.205 | 77.413 |
| 100.000 | 61.232 | 59.482 | 3.000 | 16 | 50 | 3.125 | 2.322 | 1.000 | 49.970 | 9.026 | 35.246 | 77.997 |
| 106.000 | 49.540 | 48.040 | 2.500 | 21 | 62 | 2.952 | 1.692 | 1.002 | 50.176 | 8.139 | 39.247 | 78.171 |
| 106.000 | 50.497 | 48.997 | | 19 | 56 | 2.947 | 1.871 | 1.001 | 50.059 | 8.282 | 38.477 | 78.382 |
| 106.000 | 50.408 | 48.908 | | 21 | 64 | 3.048 | 1.801 | 1.001 | 50.069 | 8.334 | 38.246 | 77.533 |
| 106.000 | 51.000 | 49.500 | 2.750 | 19 | 58 | 3.053 | 1.958 | 1.001 | 50.107 | 8.417 | 37.897 | 77.659 |
| 106.000 | 52.974 | 51.474 | 3.000 | 17 | 52 | 3.059 | 2.135 | 0.998 | 49.786 | 8.763 | 36.167 | 78.341 |
| 106.000 | 52.951 | 51.451 | 3.000 | 17 | 53 | 3.118 | 2.174 | 0.998 | 49.790 | 8.785 | 36.083 | 77.960 |
| 106.000 | 54.602 | 53.102 | 3.000 | 17 | 54 | 3.176 | 2.242 | 1.000 | 49.962 | 9.090 | 34.992 | 77.691 |
| 106.000 | | 54.472 | | 18 | 57 | 3.167 | 1.954 | 0.999 | 49.944 | 9.394 | 33.846 | 78.568 |
| 106.000 | | 54.497 | | 19 | 59 | 3.105 | 2.282 | 0.994 | 49.445 | 9.367 | 33.605 | 77.251 |
| 106.000 | | 59.696 | | 16 | 52 | 3.250 | 2.309 | 0.999 | 49.894 | 10.359 | | 79.068 |
| 111.292 | | 42.920 | | 25 | 78 | 3.120 | 1.492 | 1.000 | 49.987 | 8.162 | 38.987 | 77.012 |
| 112.000 | | 41.484 | | 25 | 74 | 2.960 | 1.471 | 0.999 | | 7.868 | | |
| 112.000 | | 42.500 | | 19 | 56 | 2.947 | 2.057 | 0.999 | | | | |
| 112.000 | | 43.468 | | 20 | 61 | 3.050 | 1.832 | 1.000 | | 8.270 | | 77.761 |
| 112.000 | | 43.817 | | 24 | 74 | 3.083 | 1.456 | 0.998 | | 8.416 | | 78.094 |
| 112.000 | | 43.994 | | 24 | 75 | 3.125 | 1.509 | 0.998 | | 8.472 | 37.424 | 77.783 |
| 112.000 | | 45.241 | | 18 | 55 | 3.056 | 2.012 | 1.000 | | 8.610 | 36.949 | 78.304 |
| 112.000 | | 45.172 | | 20 | 62 | 3.100 | 1.916 | 0.998 | | 8.617 | 36.787 | 77.521 |
| 112.000 | | 46.532 | | 18 | 57 | 3.167 | 2.129 | 1.000 | | 8.904 | 35.716 | 77.668 |
| 112.000 | | 47.375 | | 23 | 68 | 2.957 | 2.025 | 0.999 | 49.903 | 9.027 | 35.193 | 76.962 |
| 112.000 | | 46.803 | | 21 | 67 | 3.190 | 1.663 | 0.999 | 49.946 | 9.056 | | 78.253 |
| 112.000 | | 46.926 | | 21 | 68 | 3.238 | 1.713 | 0.999 | | 9.104 | | 77.924 |
| 112.000 | | 48.239 | | 19 | 60 | 3.158 | 1.846 | 0.999 | 49.932 | 9.298 | 34.186 | 78.712 |
| 112.000 | | 51.655 | | 17 | 55 | 3.235 | 2.150 | 0.999 | 49.899 | 10.008 | 31.741 | 78.996 |
| 118.000 | | 39.919 | | 25 | 79 | 3.160 | 1.423 | 0.999 | 49.928 | 8.575 | | 77.918 |
| 118.000 | | 40.451 | 2.250 | 25 | 78 | 3.120 | 1.383 | 0.999 | 49.400 | 8.666 | | 78.256 |
| 118.000 | | 40.469 | | 25 | 80 | 3.200 | 1.474 | 0.993 | 49.330 | 8.715 | | 77.669 |
| 118.000 | | 43.663 | | 24 | 78 | 3.250 | 1.443 | 0.999 | 49.881 | 9.472 | 33.524 | 78.792 |
| 118.000 | | 44.349 | | 25 | 81 | 3.240 | 1.744 | 1.001 | 50.105 | 9.632 | 33.115 | 77.328 |
| 141.955 | | 25.920 | 4.320 | 16 | 49 | 3.063 | 2.266 | 1.000 | 50.009 | 7.923 | | 77.413 |
| 161.648 | 20.260 | 18.700 | 3.117 | 25 | 78 | 3.120 | 1.447 | 1.000 | 50.014 | 7.545 | 42.201 | 77.012 |



Combination of goals: high power density at low size

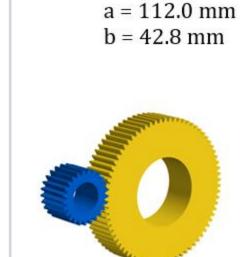
Smallest size

High power density low size

Smallest weight

a = 97.7 mm

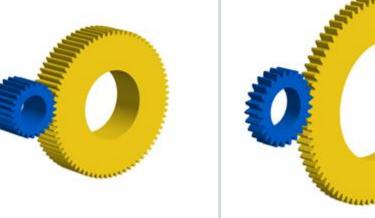
b = 60.9 mm

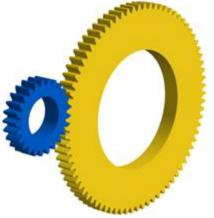


a = 161.6 mm

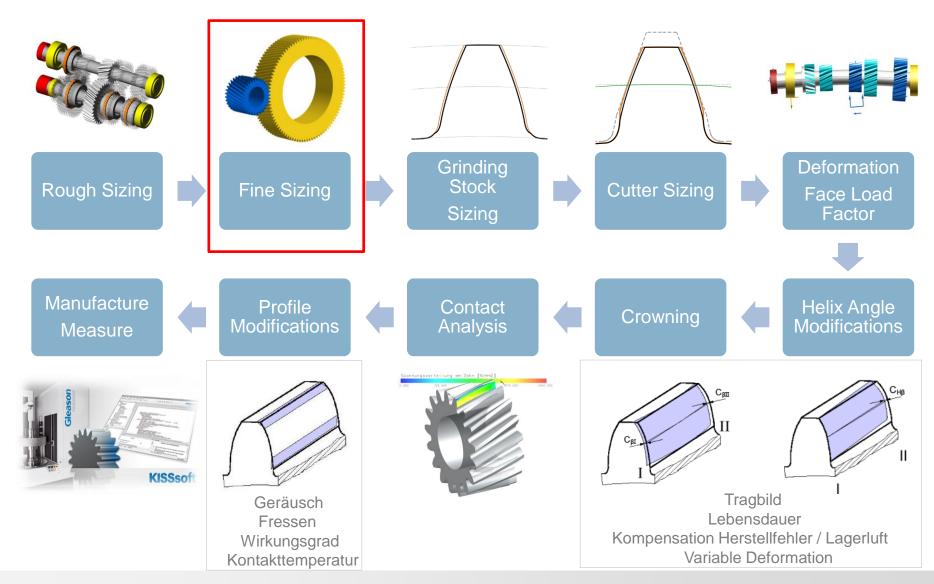
b = 20.3 mm



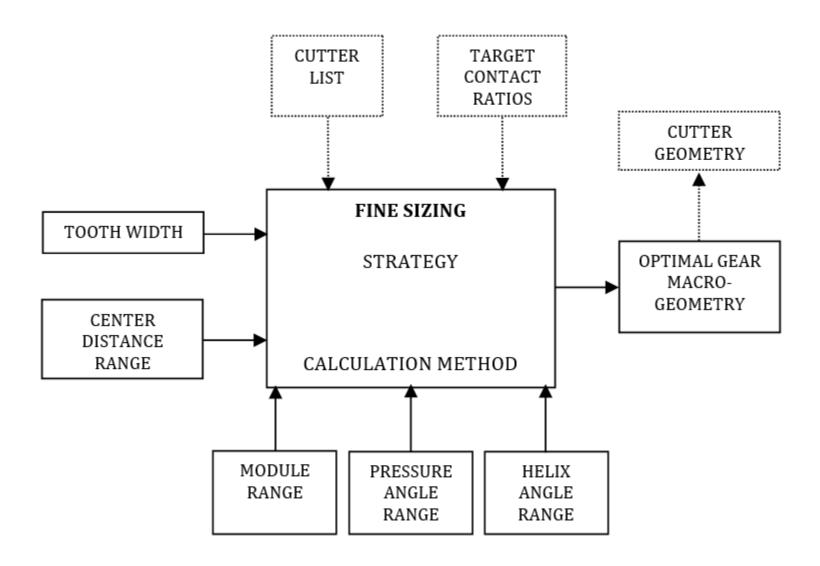












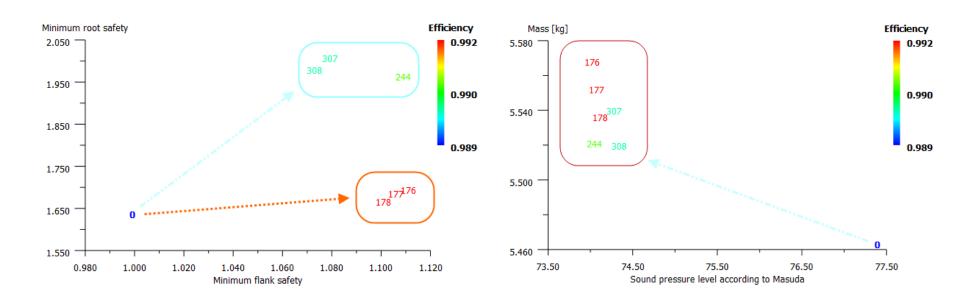


Fine Sizing

Goal: optimal gear macro-geometry

Possible Target:

Find a solution with high Safety Factors, low Weight, low Noise Excitation (high contact ratio) and high Efficiency.



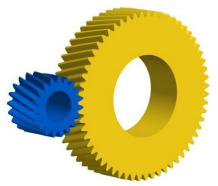


Fine Sizing

The consideration of available cutters in the early design process can save a lot of effort in further design steps.

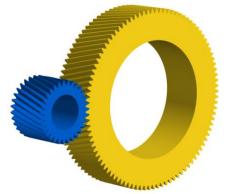
Standard cutter profile: ISO 53 Profil A

- Standard cutter (lower costs)
- Lower contact ratio
- Lower root stresses
- Higher noise excitiation

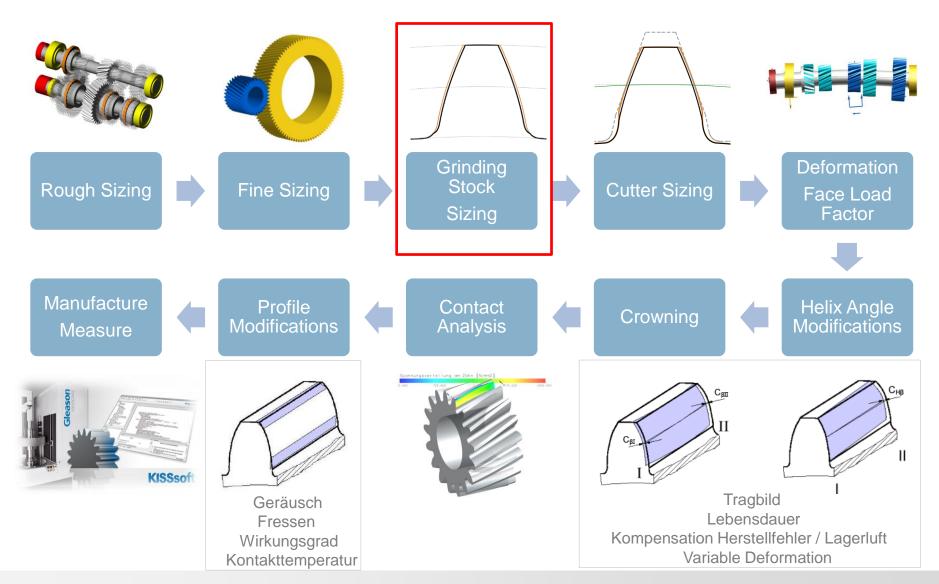


Deep Tooth Form

- Special cutter (higher costs)
- Higher contact ratio
- Higher root stresses
- Lower noise excitation









Sizing of grinding stock

$$q = q_1/4 + \sqrt{(q_2/4)^2 + V_E^2 + (F_\alpha/2)^2 + (F_\beta/2)^2 + (F_\beta/2)^2}$$

- q = Nennwert des anzustrebenden Aufmaßes pro Flanke
- q₁ = Zahnweitentoleranz der Fertigbearbeitung (Wkmax. Wkmin.)
- q₂ = Zahnweitentoleranz der Vorbearbeitung (Wkmax. Wkmin.)
- V_E = angenommener Versatz der Links- zu Rechtsflanken (für Honprozess hier keine Eingabe / für Schleifprozess sollten ca. 15µm angesetzt werden)
- F_α = Profil Gesamtabweichung der Vorbearbeitung)*
- Fß = Flankenlinien Gesamtabweichung der Vorbearbeitung)*
- Fp = Teilungs Gesamtabweichung der Vorbearbeitung)*

 für Schleifprozess wird 100% des Fp-Betrages angesetzt, für Honprozess wird je nach Bearbeitungsstrategie 30 bis 60% des Fp-Betrages der Vorbearbeitung angesetzt
 -)* wenn keine IST-Werte bekannt, dann DIN Q 9,5 ansetzen

Alle Werte in µm

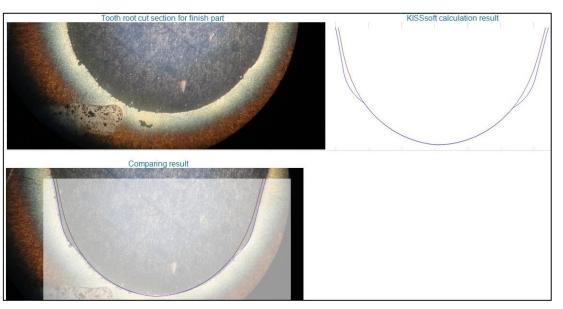


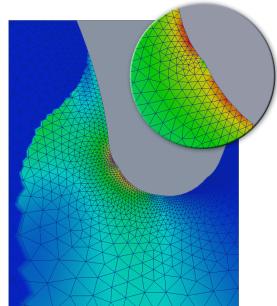
Sizing of grinding stock

If the flank is ground and the root not, a **grinding notch** will appear in the root area.

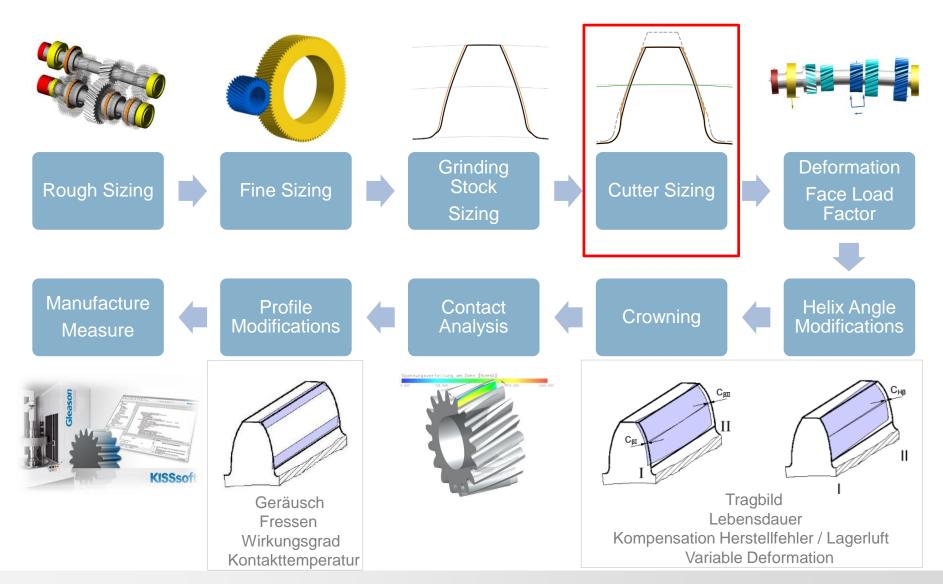
Due to the notch effect, the root stresses will increase.

In order to avoid the grinding notch, a protuberance cutter is designed.



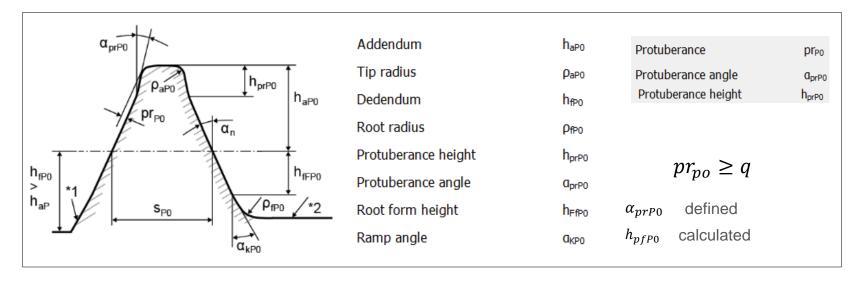


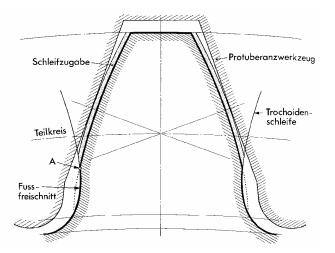


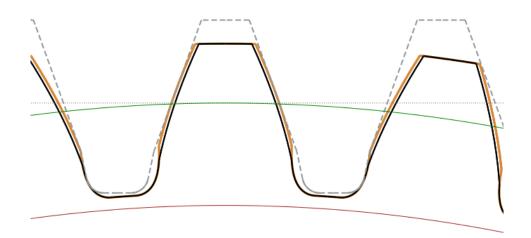




Sizing of protuberance cutter





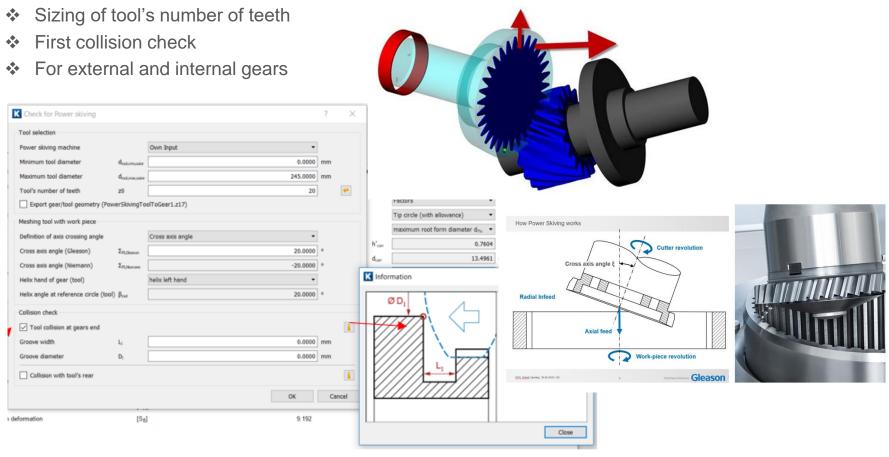




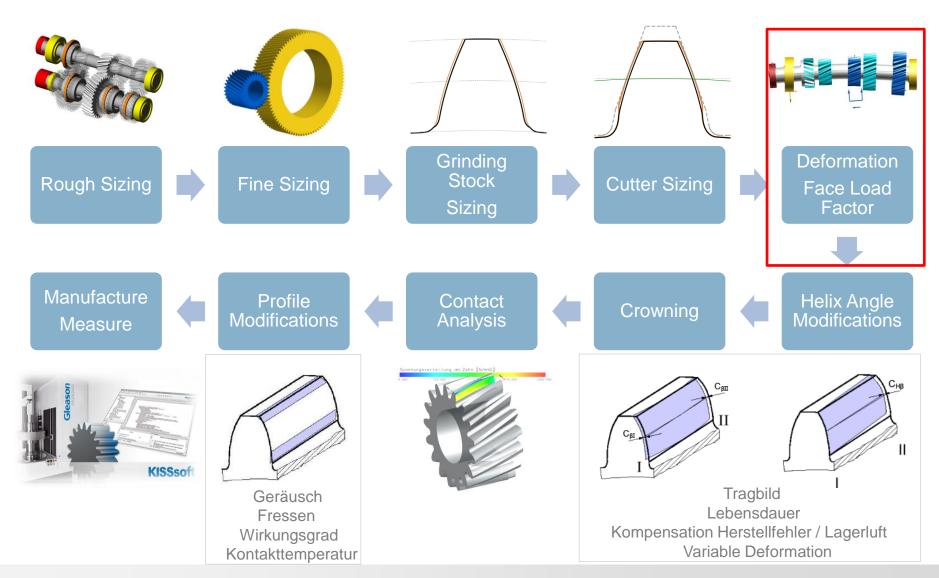
Feasibility assessment for Power-Skiving

KISSsoft performs a feasibility assessment for manufacturing Power-Skiving

Checks if a given gear can be manufacturing by Power-Skiving



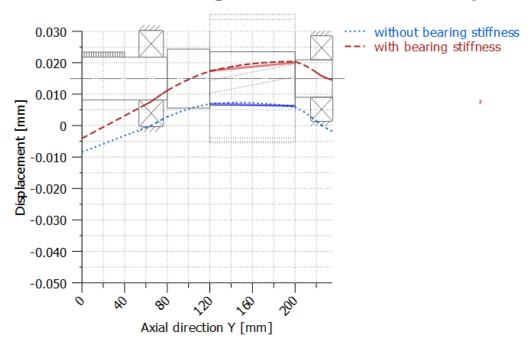






Calculation of deformation

Example: Influence of **Bearing Stiffness** on shaft **Displacement**

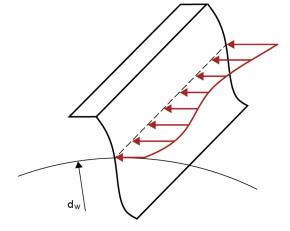


The gear inclines due to shaft deformation. If not compensated by lead modifications, this will result in an uneven load distribution on the tooth flank.



Definition of the Face Load Factor $K_{H\beta}$ (ISO 6336-1)

$$K_{H\beta} = \frac{maximum\ line\ load}{average\ line\ load}$$



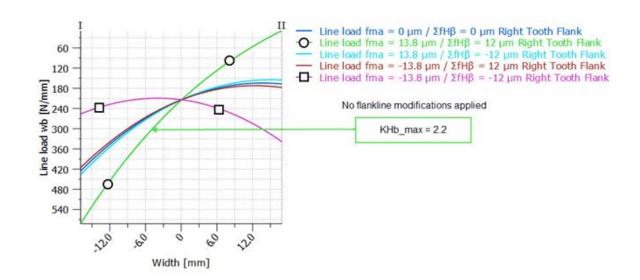
Considers shaft deformation and flankline ISO 6336-1 Annex E: modifications



Calculation of face load factor with manufacturing allowances

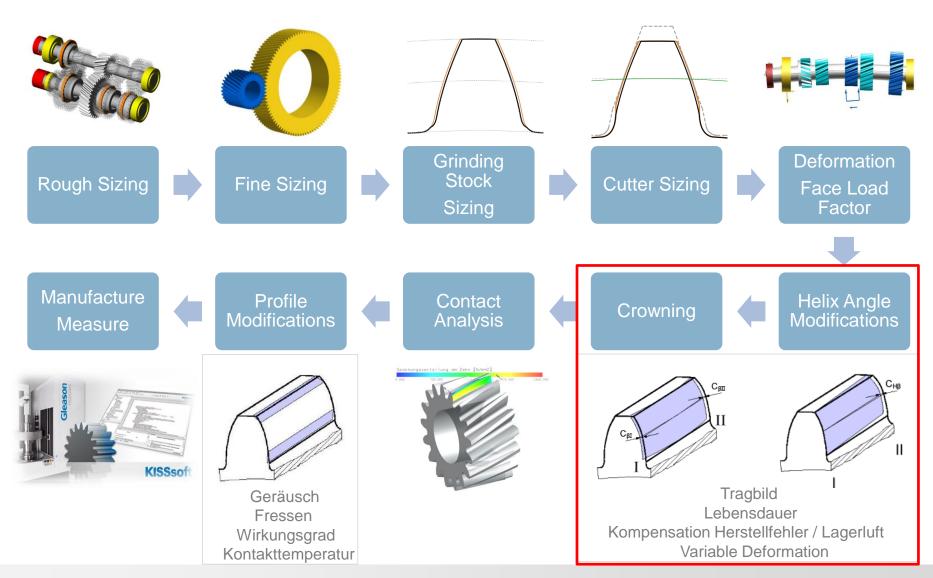
Manufacturing errors like axis non-parallelism (f_{mq}) und helix slope deviation $(f_{H\beta})$ can be considered in the calculation. Since manufacturing errors can have either a positive or a negative sign, several scenarios must be analysed.

- $f_{ma} = 0$ and $f_{H\beta} = 0$
- f_{ma} (+) and $f_{H\beta}$ (+)
- f_{ma} (+) and $f_{H\beta}$ (-)
- f_{ma} (-) and $f_{H\beta}$ (+)
- f_{ma} (-) and $f_{H\beta}$ (-)



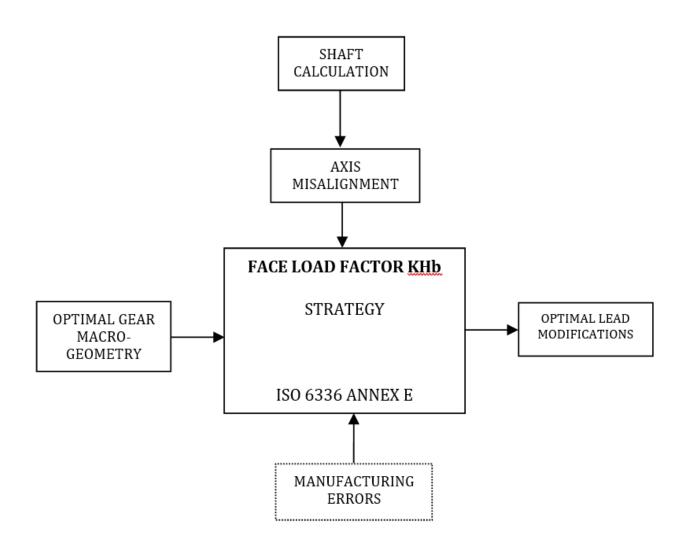
According to ISO 6336, Annex E, the strength calculation must be performed with the highest face load factor (in this example, KH β =2.2) that results from the above 5 cases.







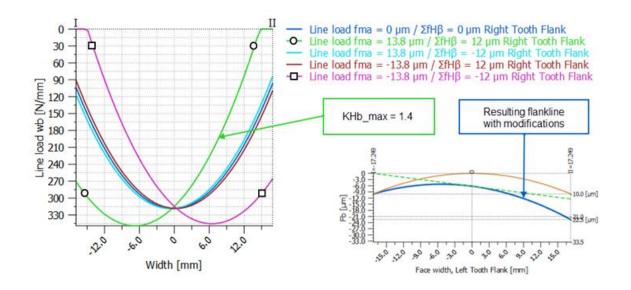
Sizing of flankline (lead) modifications with manufacturing constraints





Sizing of flankline (lead) modifications with manufacturing constraints

In order to optimize the load distribution along the face width with manufacturing errors, often a crowning C_{β} and a helix angle modification $C_{H\beta}$ is introduced.

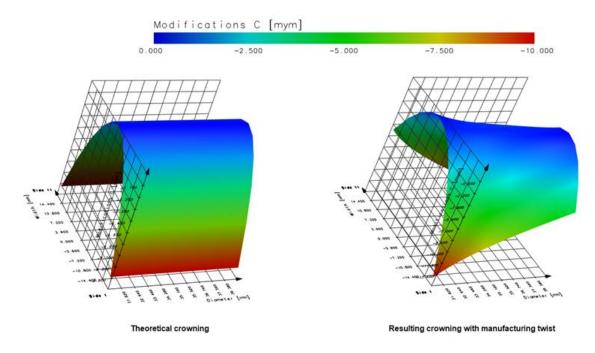


Conclusion: Flankline modifications are used to optimize the line load distribution. In this example, the face load factor was reduced from 2.2 down to 1.4. Applying the resulting face load factor in the strength calculation resulted in 45% higher root safety and 20% higher flank safety.



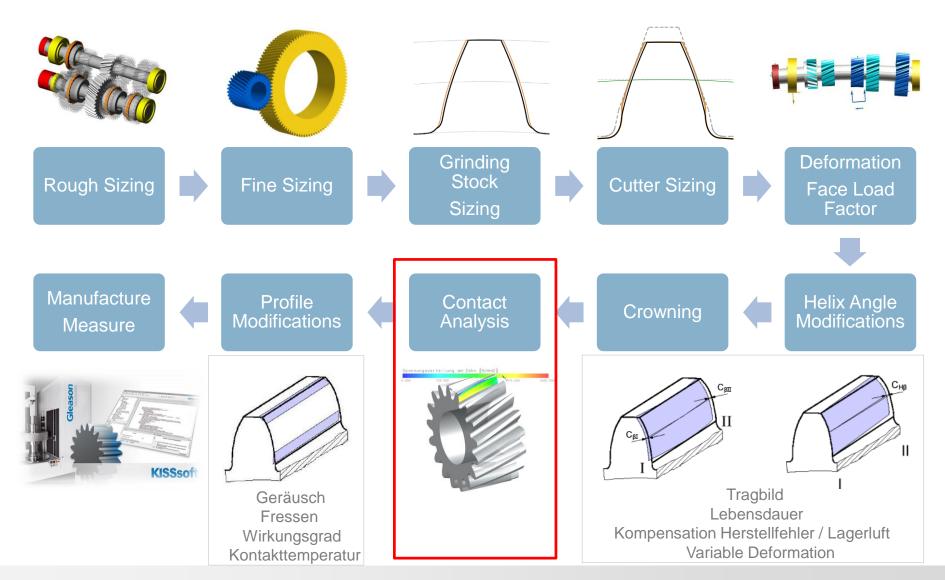
Twist due to manufacturing

When using generation grinding to produce crowning in helical gears, a twist may appear due to the grinding motion of the tool. If not compensated, this may lead to a higher effective line load.



The twist due to manufacturing can be estimated in KISSsoft and applied for a detailed contact analysis.

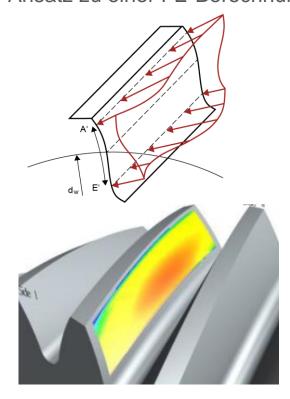


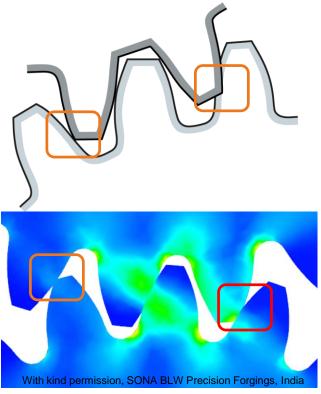




Loaded Tooth Contact Analysis (LTCA)

Die Kontaktanalyse rechnet die Zahndeformation unter Last und die Spannungen über den gesamten Eingriff und Zahnbreite. Die Berechnung basiert auf dem FVA-Bericht 129 und 134 nach Weber und Banaschek und ist ein alternativer Ansatz zu einer FE-Berechnung.





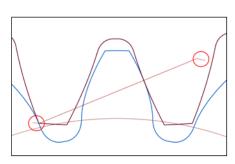


Loaded Tooth Contact Analysis (LTCA)

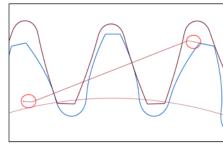
A loaded tooth contact analysis evaluates the meshing under loaded conditions. Important parameters such as:

- Contact Shocks
- Transmission error (TE)
- Amplitude spectrum of TE
- Contact ratio under load are calculated.

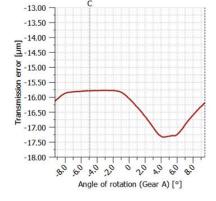
What is the optimal profile modification?



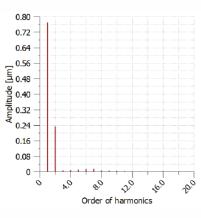
Contact shock (example profile C)



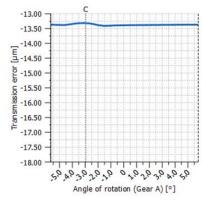
Contact shock (example deep tooth form)



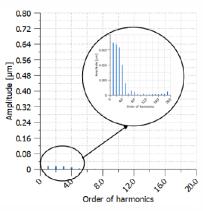
TE (example Profile C)



TE Harmonics (example Profile C)

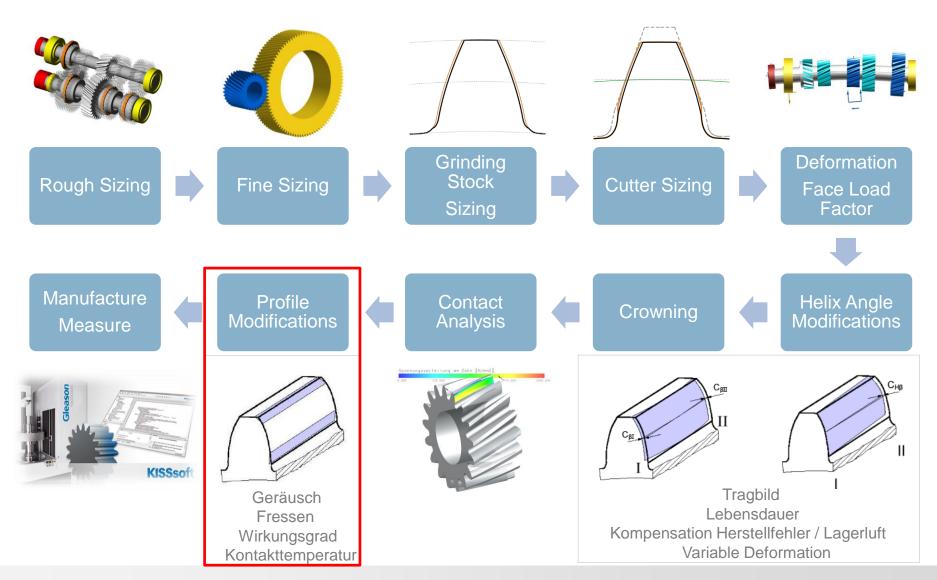


TE (example deep tooth form)



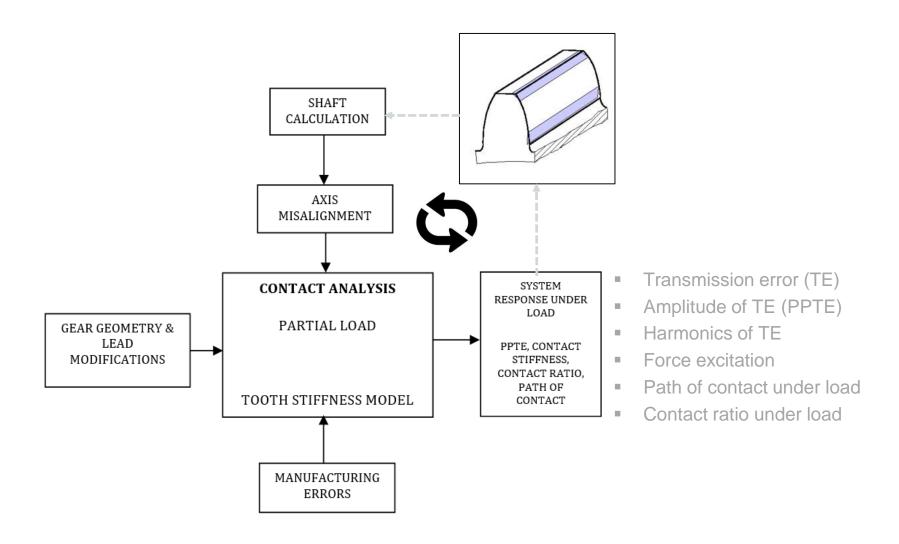
TE Harmonics (example deep tooth form)







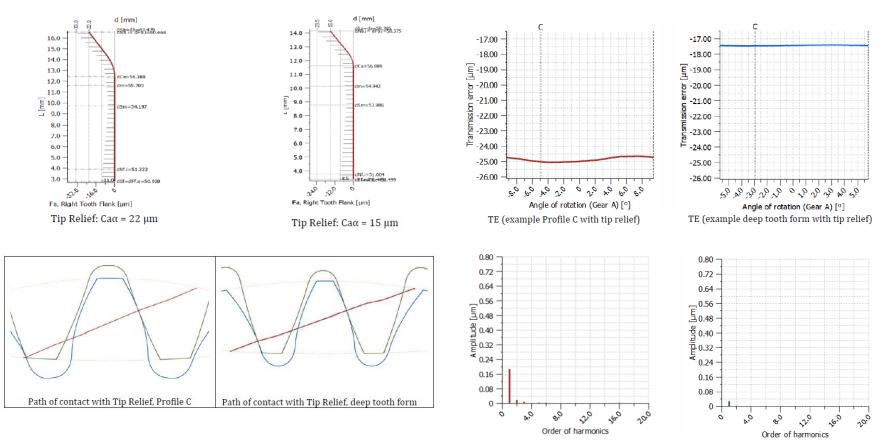
Sizing of profile modifications





Sizing of profile modifications

An optimal profile modification eliminates contact shocks, reduces the peak-topeak transmission error and eliminates higher orders of harmonics, to ensure a smooth transmission error curve that is similar to a sin-wave.



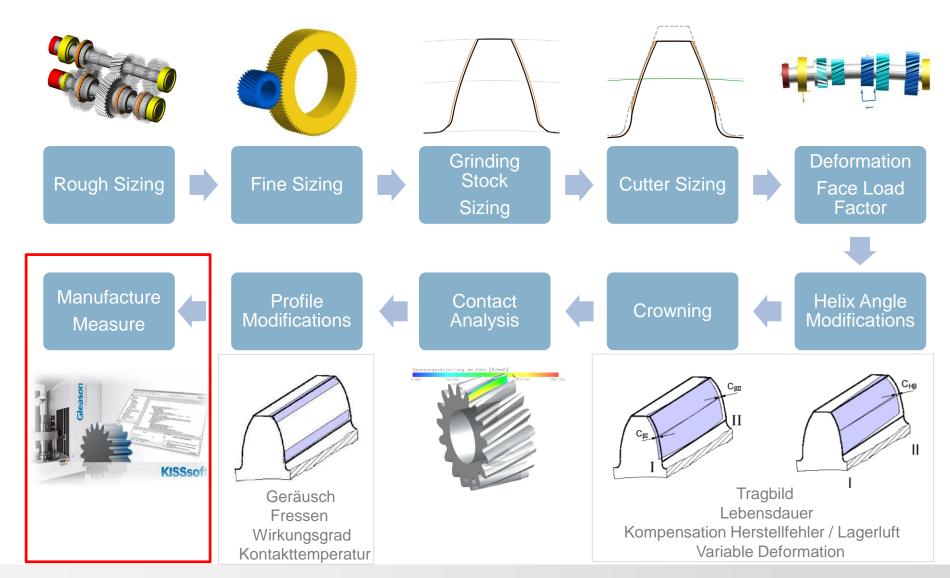
Sizing of profile modifications

In KISSsoft, it is possible to assess which modifications can be manufacturing by a list of available **Dressing Wheels** or **Grinding Worms**.

Considering existing tools in the design process may further reduce manufacturing costs during the grinding process.

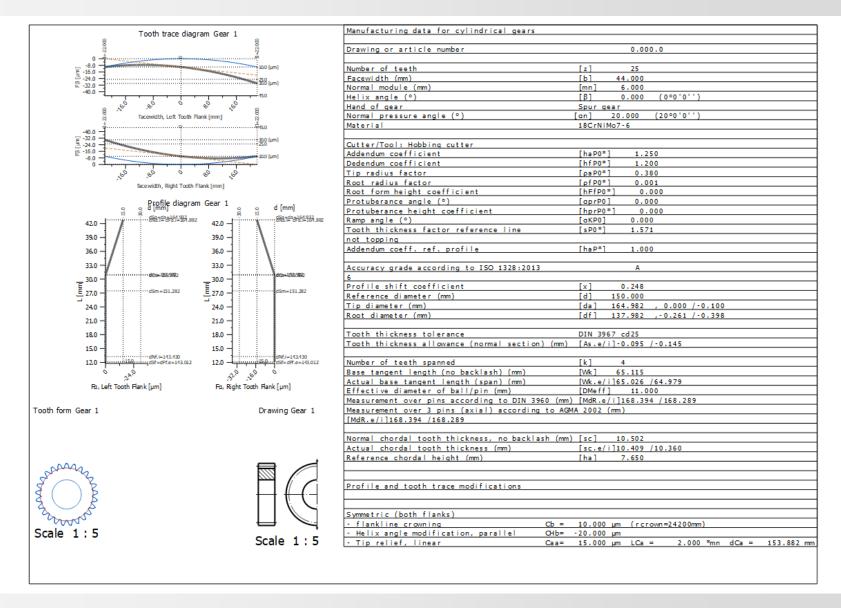






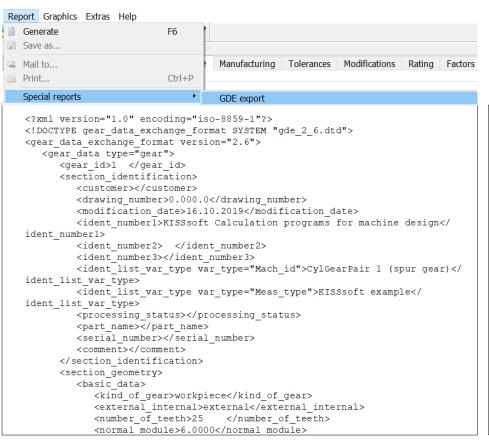


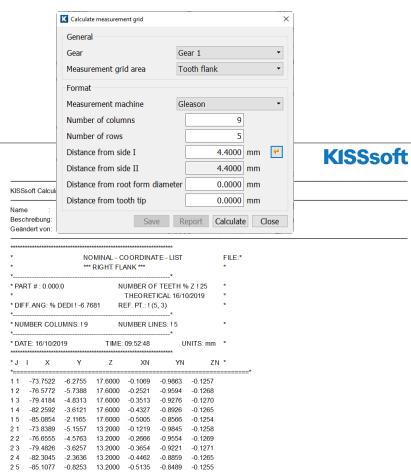
Manufacturing Data





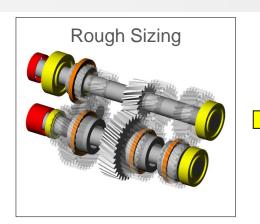
Measurement Data (GDE / Measurement Grid)

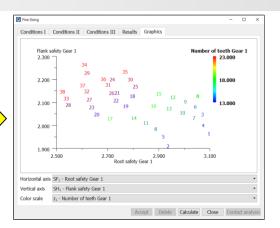


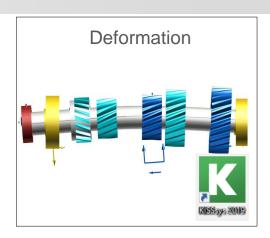




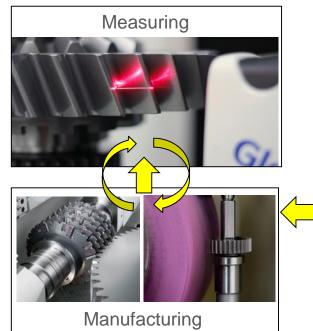
Summary



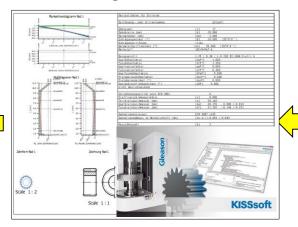




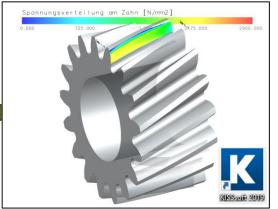
Fine Sizing



Manufacturing & Measurement Data

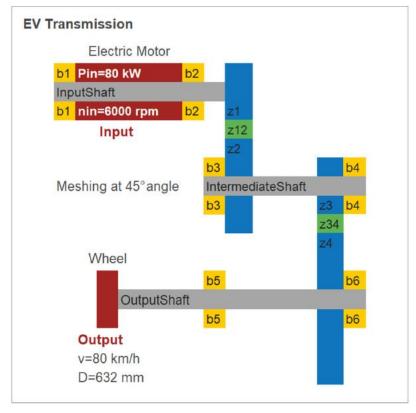


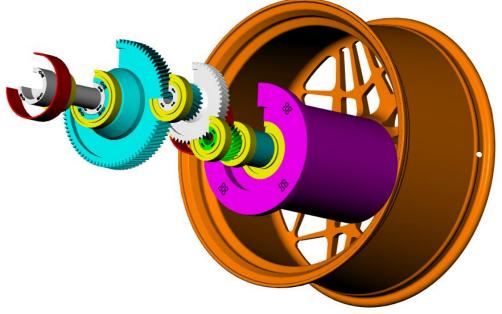
Contact Analysis
Micro-Geometry





Calculation Example







Calculation Example

Calculation Methods

Gears: ISO 6336 SHmin = 1.1 SFmin = 1.6

Shafts: DIN 743 SSmin = 1.2 SDmin = 1.2 Shafts: C45

Bearings: ISO 16281 Hmin = 5000h Housing: Aluminium

Lubrication

Oil Injection, ISO VG 46, 80°

$$i = \frac{n_{motor \cdot D \cdot \pi}}{v}$$

i... Transmission ratio, n_{motor} ... Optimal motor RPM [1/min],

D... Outer tire diameter [m], v... Average vehicle speed [m/min]

Example:
$$i = \frac{6000 \ rpm \cdot 0.632 \ m \cdot 3.14}{1333 \cdot \frac{m}{min}} = 8.9$$

$$i_{12}$$
= 2.3 i_{34} = 3.7

Materials

Gears: 18 CrNiMo7-6 Case Hardened

References

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Thank you for your attention!

Sharing Knowledge

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