

# KISSsoft Exercise 3

## Bevel Gear 03

Sizing of a Face Hobbing hypoid gearset

# 1 Purpose of exercise

In this exercise, we will design a Face hobbing bevel gearset, then change it into a hypoid gearset. It is an industrial application, lapped.

- Sizing of a new bevel gear set
- Selection of the size of cutter head and check the influence to the root strength
- Comparison of a bevel gear to a hypoid gear regarding strength and efficiency
- Optimization of hypoid gear set using fine sizing

## 2 Task

### Initial data:

Bevel type: Face hobbing, lapped  
Material: 16 MnCr5  
Oil: ISO VG 68, oil bath  
Gear quality: 8 as per ISO 17485  
Hand of spiral: Pinion left hand (LH)

Rating standard: ISO 10300:2014  
Power:  $P = 24 \text{ kW}$   
Speed (at pinion):  $n = 3'000 \text{ upm}$   
Required lifetime: 5000 h  
Operation mode: Drive side

Application factor:  $K_A = 1.1$   
Mounting factor:  $K_{H\beta\text{-be}} = 1.1$

Manufacturing process: Ring gear non-generating

### 2.1 Step 1

Do a first sizing using the functionality „Rough sizing“. Check the strength at the bevel gear set (without offset).

### Sizing data:

The required safeties are  $S_{Fmin} = 1.4$  and  $S_{Hmin} = 1$ .

Transmission ratio: 3.9  
Gear set ratios:  $b/m_n = 10$ ,  $R_e/b = 3.0$   
Spiral angle:  $30^\circ$

Cutter head size: Sizing with ratio of involute / outer cone distance = 0.9

### 2.2 Step 2

Choose the cutter head from the list of ISO 23509. The smallest possible cutter head is to be preferred, due to the positive V/H (E/P) behavior and benefit to the root strength.

Compare the root safety SF in ISO 10300, if the bigger cutter head is taken instead of the smaller cutter head.

## 2.3 Step 3

Change the calculation to hypoid and add the offset. Define the blanks. Compare the strength and the blanks in 2D graph „System“.

The offset is 15% of the ring gear outer diameter.

## 2.4 Step 4

Optimize the hypoid design with the „fine sizing“ functionality. Check for an optimal solution with same ring gear diameter.

### Sizing data:

Offset:                      between 10% and 25% of ring gear outer diameter

The focus of the optimization should be on pinion root strength and efficiency (method acc. to WECH). Second priority are high contact ratio (for noise) and low axial forces on pinion.

## 3 Solution

### 3.1 Step 1

Input of initial data

In tab “Basic data”, select the following gear geometry settings:

Basic data | Process | Reference profile | Manufacturing

Configuration

Type: Uniform depth, fig 3 (Face Hobbing, Klingelnberg)

Normal pressure angle  $\alpha_n$ : 20.0000°

Gear 1: helix left hand (spiral teeth)

Mean spiral angle Gear 2  $\beta_{m2}$ : 30.0000°

Quality (ISO 17485) Q: 8 8

Figure 3.1-1 Choose “Uniform depth” in tab «Basic data», set hand of spiral and enter the gear quality number.

Select the gear material and use a lubricant as shown below:

Material and lubrication

Gear 1: Case-hardening steel | 16 MnCr 5 (1), case-hardened, ISO 6336-5 Figure 9/10 (MQ), Core hardness >=25HRC Jominy J=12mm<HR(

Gear 2: Case-hardening steel | 16 MnCr 5 (1), case-hardened, ISO 6336-5 Figure 9/10 (MQ), Core hardness >=25HRC Jominy J=12mm<HR(

Lubrication: Oil bath lubrication | Oil: ISO-VG 68

Figure 3.1-2 Gear material and lubrication in tab «Basic data»

Define the load data and select the rating method in tab “Strength”.

Note that the working flank is initially defined as right flank, which results in ‘Coast’ condition. Change the working flank gear 1 to ‘left flank’.

Basic data | Process | Reference profile | Manufacturing | Tolerances | Strength | Factors

Rating

Driving gear: Gear 1

Working flank Gear 1: left flank

Sense of rotation, looking at tip of Gear 1: left

Operation: Drive side

Required service life: 5000.0000 h

Calculation method

Factors, root, flank: Bevel gear ISO 10300:2014, Method B1

Scuffing: according to calculation method

Tooth flank fracture: No calculation

Reference gear: Gear 1

Reference speed  $|n_1|$ : 3000.0000 1/min

Reference torque  $|T_1|$ : 76.3944 Nm

Reference power  $|P|$ : 24.0000 kW

Subsurface fatigue: DNV 41.2

Reliability: No calculation

Figure 3.1-3 Select rating method ISO 10300:2014 B1, enter power and speed and set required life to 5000 h. Also change the working flank to ‘left flank’.

In the tab “Factors”, the application factor and mounting factor are defined.

| General factors                              |                 |  |        |   |
|----------------------------------------------|-----------------|--|--------|---|
| Application factor                           | $K_A$           |  | 1.1000 | ? |
| Dynamic factor                               | $K_v$           |  | 1.0885 | ? |
| Transverse load factor                       | $K_{H\alpha}$   |  | 1.8262 | ? |
| Mounting factor (Load distribution modifier) | $K_{H\beta-be}$ |  | 1.1000 | ? |

Z-Y Factors

Figure 3.1-4 Set mounting factor  $K_{H\beta-be} = 1.10$  and the application factor  $K_A = 1.10$ .

Before sizing of the bevel gear, the required safeties are to be entered.

Under 'calculation – settings' the required safeties are defined. For an easier display, the option 'Safeties are not depending on size' may be used.

| Module specific settings                       |             |                                |        |
|------------------------------------------------|-------------|--------------------------------|--------|
| General                                        |             |                                |        |
| Configuration                                  |             | Safeties not depending on size |        |
| Required safeties for metal (ISO/DIN)          |             |                                |        |
| Root safety                                    | $S_{Fmin}$  |                                | 1.4000 |
| Flank safety                                   | $S_{Hmin}$  |                                | 1.0000 |
| Safety against scuffing (integral temperature) | $S_{Smin}$  |                                | 1.8000 |
| Safety against scuffing (flash temperature)    | $S_{Bmin}$  |                                | 2.0000 |
| Safety against tooth flank fracture            | $S_{FFmin}$ |                                | 1.2000 |

Figure 3.1-5 Enter the required safety factors in 'module specific settings'.

Now we start using the rough sizing function. Enter the required ratio and the mean helix angle at  $30^\circ$ , press "Calculate" and "Accept".

| Rough sizing macrogeometry          |              |  |             |
|-------------------------------------|--------------|--|-------------|
| Transmission ratio                  | $u$          |  | 3.9         |
| Ratio of facewidth to normal module | $b/m_{mn}$   |  | 10.0000     |
| Ratio of cone distance to facewidth | $R_e/b$      |  | 3.0000      |
| Mean spiral angle Gear 2            | $\beta_{m2}$ |  | 30.0000 °   |
| Mean normal module                  | $m_{mn}$     |  | 2.9414 mm   |
| Number of teeth, Gear 1             | $z_1$        |  | 11          |
| Facewidth Gear 2                    | $b_2$        |  | 30.1504 mm  |
| Outer pitch diameter Gear 2         | $d_{e2}$     |  | 175.2588 mm |

Accept Calculate Cancel

Figure 3.1-6 Use of rough sizing function to get a first proposal for the bevel gear set

You will see that the pinion number of teeth is reasonable (a reasonable range is e.g. 11-16). In the tab "Process", set up the manufacturing process for ring gear as formate (non-generating) and use the sizing button for the cutter head.

Basic data | Process | Reference profile | Manufacturing | Tolerances | Strength

Manufacturing process

Gear 1      Gear 2

Manufacture type   generate      formate

Process      hipped

Manufacturer's data for spiral teeth

☐ Adopt data from Klingelnberg machines list

Manufacturing      Face Hobbing (continuing indexing method)

Cutter radius       $r_{c0}$       45.2256 mm

Number of blade groups  $z_0$       1.0000

Cutter module       $m_0$       3.2000 mm

K Convert cutter radius

☐ Cutter radius according to  $r_{c0}/R_{m2}$

☒ Cutter radius according to involute/ $R_{e2}$

Ratio involute/outer cone distance      0.9000

Cutter radius       $r_{c0}$       49.2070 mm

Accept      Calculate      Cancel

Cutter radius       $r_{c0}$       49.2070 mm

Number of blade groups  $z_0$       1.0000

Cutter module       $m_0$       3.2000 mm

Figure 3.1-7 Setting of manufacturing process and sizing of cutter head with ratio involute / outer cone = 0.9.

The strength results can be checked now. Due to the simplified sizing algorithm, deviations from the required safety values may show up.

| Results (basic calculation)             |                    |        |         |
|-----------------------------------------|--------------------|--------|---------|
| General                                 |                    |        |         |
| Transverse contact ratio                | $[\epsilon_d]$     | 1.234  |         |
| Overlap ratio                           | $[\epsilon_\beta]$ | 1.387  |         |
| Operation mode                          | Drive side         |        |         |
| Components                              |                    | Gear 1 | Gear 2  |
| Outer tip diameter (mm)                 | $[d_{ae}]$         | 52.984 | 176.090 |
| Root safety                             | $[S_F]$            | 2.336  | 1.979   |
| Flank safety                            | $[S_H]$            | 0.997  | 1.040   |
| Safety factor for scuffing (flash-temp) | $[S_B]$            | 4.118  |         |

Figure 3.1-8 Bevel gear safety factors after rough sizing.

See file [Exercise-Bevel-03-sizing\\_hypoid\\_face\\_hobbing-v2200-jl-public\\_Step-1.Z70](#)

## 3.2 Step 2

The cutter head size is the nominal radius, on which the blades of the tool are arranged. They come with standard sizes.



Figure 3.2-1 Face Hobbing cutter head. Radius is defined from center to the cutting edge of the blade.

In tab "Process", the info graphic for the tools according to the ISO 23509 is available.

| Face Hobbing                                          |                                  | Face Milling                              |
|-------------------------------------------------------|----------------------------------|-------------------------------------------|
| Two-blade cutter<br>(outer and inner blade per group) |                                  |                                           |
| Cutter radius<br>$r_{c0}$ , mm                        | Number of blade<br>groups, $z_0$ | Cutter diameter,<br>$2 \cdot r_{c0}$ , in |
| 30                                                    | 7                                | 2.50                                      |
| 51                                                    | 7                                | 3.25                                      |
| 64                                                    | 11                               | 3.50                                      |
| 64                                                    | 13                               | 3.75                                      |
| 76                                                    | 7                                | 4.375                                     |
| 76                                                    | 13                               | 5.00                                      |
| 76                                                    | 17                               | 6.00                                      |
| 88                                                    | 11                               | 7.50                                      |
| 88                                                    | 17                               | 9.00                                      |
| 88                                                    | 19                               | 10.5                                      |
| 100                                                   | 5                                | 12                                        |
| 105                                                   | 13                               | 14                                        |
| 105                                                   | 19                               | 16                                        |
| 125                                                   | 13                               | 18                                        |
| 150                                                   | 17                               | /                                         |
| 175                                                   | 19                               | /                                         |
|                                                       |                                  | mm                                        |
|                                                       |                                  | 500, 640, 800, 1000                       |

Figure 3.2-2 Available cutter radius of standardized cutter heads

We choose the smallest possible cutter due to the centralized contact pattern behaviour under load.

Cutter radius

$r_{c0}$ 
 mm

Number of blade groups

$z_0$

Cutter module

$m_0$ 
 mm
☐

Figure 3.2-3 Enter the cutter radius and the number of blades in tab "Process".

With this we have finalized the design and manufacturing of a bevel gear set (not a hypoid yet). Rerun the calculation to find:

| Results (basic calculation)             |                     |        |         |
|-----------------------------------------|---------------------|--------|---------|
| General                                 |                     |        |         |
| Transverse contact ratio                | $[\epsilon_\alpha]$ | 1.234  |         |
| Overlap ratio                           | $[\epsilon_\beta]$  | 1.387  |         |
| Operation mode                          | Drive side          |        |         |
|                                         |                     |        |         |
| Components                              |                     | Gear 1 | Gear 2  |
| Outer tip diameter (mm)                 | $[d_{ae}]$          | 53.994 | 179.447 |
| Root safety                             | $[S_F]$             | 2.459  | 2.083   |
| Flank safety                            | $[S_H]$             | 0.996  | 1.039   |
| Safety factor for scuffing (flash-temp) | $[S_B]$             | 3.919  |         |

Figure 3.2-4 Gear rating results with above manufacturing data.

See file [Exercise-Bevel-03-sizing\\_hypoid\\_face\\_hobbing-2200-jl-public\\_Step-2.Z70](#)

### 3.3 Step 3

We now compare a bevel gear set with a hypoid gear set. For the current bevel design, we find the efficiency according to calculation method “Wech”. To calculate the efficiency of the bevel gear set with the method “Wech”, we deactivate the scuffing calculation and select the method “Wech” in the module specific settings.

#### 14.2 Gear power loss and coefficient of friction

|                                                                               |             |        |
|-------------------------------------------------------------------------------|-------------|--------|
| Calculation according to                                                      | Wech        |        |
| Coefficient of friction                                                       | $[\mu_m]$   | 0.073  |
| The coefficient of friction $\mu_m$ can vary depending on calculation method. |             |        |
| Compound velocity (m/s)                                                       | $[v\Sigma]$ | 6.951  |
| Loss factor                                                                   | $[1/\eta]$  | 0.180  |
| Gear power loss (kW)                                                          | $[PVZ]$     | 0.314  |
| Meshing efficiency (%)                                                        | $[\eta_z]$  | 98.691 |

Figure 3.3-1 Report, information on efficiency, for bevel gear set

Now we enter an offset of 15% (here 27 mm) to calculate a corresponding hypoid gear set. We now observe a massive increase in root safety due to the hypoid offset. Due to the increased diameter of the pinion, lower forces result.

|                                     |           | Gear 1   | Gear 2  |                          |
|-------------------------------------|-----------|----------|---------|--------------------------|
| Number of teeth                     | $z$       | 11       | 43      |                          |
| Facewidth                           | $b$       | 37.0000  | 30.7253 | mm                       |
| Profile shift coefficient           | $x_{hmn}$ | 0.4300   | -0.4300 | ↔                        |
| Tooth thickness modification factor | $x_{smn}$ | 0.0650   | -0.0650 | <input type="checkbox"/> |
| Quality (ISO 17485)                 | $Q$       | 8        | 8       | ⚙                        |
| Shaft angle                         | $\Sigma$  | 90.0000° |         |                          |
| Hypoid offset                       | $a$       | 27.0000  |         | mm                       |

Figure 3.3-2 Enter the hypoid offset of 27mm.



|                      |                                        |
|----------------------|----------------------------------------|
| Calculation method   |                                        |
| Factors, root, flank | Hypoid gears ISO 10300:2014, Method B1 |
| Scuffing             | ISO/TS 10300-20:2021                   |
| Tooth flank fracture | No calculation                         |

Figure 3.3-3 Change the calculation method in the tab 'strength' from bevel results for hypoid gear set.

| Results (basic calculation)             |                       |        |         |
|-----------------------------------------|-----------------------|--------|---------|
| General                                 |                       |        |         |
| Transverse contact ratio                | $[\epsilon_{\alpha}]$ | 1.080  |         |
| Overlap ratio                           | $[\epsilon_{\beta}]$  | 1.682  |         |
| Operation mode                          | Drive side            |        |         |
| Components                              |                       |        |         |
| Outer tip diameter (mm)                 | $[d_{ae}]$            | Gear 1 | Gear 2  |
| Root safety                             | $[S_F]$               | 75.106 | 180.137 |
| Flank safety                            | $[S_H]$               | 4.687  | 3.889   |
| Safety factor for scuffing (flash-temp) | $[S_B]$               | 1.567  | 1.634   |
|                                         |                       | 2.956  |         |

Figure 3.3-4 Increased safety numbers for hypoid gear set for root bending strength and contact stress.

In the 2D system graphics we can now clearly see the increased size of the pinion:

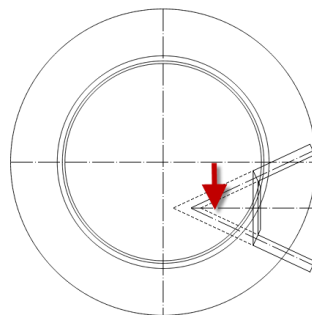


Figure 3.3-5 Increased pinion size for hypoid gear set.

The hypoid gear shows a drop in efficiency and the scuffing safety (see report):

#### 14.2 Gear power loss and coefficient of friction

|                                                                               |            |        |
|-------------------------------------------------------------------------------|------------|--------|
| Calculation according to                                                      | Wech       |        |
| Coefficient of friction                                                       | $[\mu_m]$  | 0.027  |
| The coefficient of friction $\mu_m$ can vary depending on calculation method. |            |        |
| Compound velocity (m/s)                                                       | $[v_S]$    | 0.016  |
| Gear power loss (kW)                                                          | $[PVZ]$    | 0.456  |
| Meshing efficiency (%)                                                        | $[\eta_Z]$ | 98.101 |

Check the influence factor of limit pressure angle under additional data.

Geometry

Mean normal module  $m_{mn}$  3.0423 mm  $\odot \leftrightarrow$

Outer pitch diameter Gear 2  $d_{e2}$  178.6005 mm  $\odot \oplus$

Normal pressure angle  $\alpha_n$  20.0000 °  $\oplus$

Gear 1

Mean spiral angle G

Angle modification (

**K Additional data for hypoid gears** ? X

Pressure angle on drive side  $\alpha_{dD}$  20.0000 °

Pressure angle on coast side  $\alpha_{dC}$  20.0000 °

Influence coefficient for limit pressure angle  $f_{lim}$  1.0000

OK Cancel

Figure 3.3-6 Input of influence coefficient of limit pressure angle under 'additional data for hypoid gears'

Also, check the several pressure angles such as 'design (nominal) pressure angle', 'generated pressure angle' and 'effective pressure angle' in the report.

## 5.2 Basic data

|                                           | ----- Gear 1 ----- | ----- Gear 2 ----- |
|-------------------------------------------|--------------------|--------------------|
| No modification at tip circle             |                    |                    |
| Overall transmission ratio                | [itot]             | -3.909             |
| Gear ratio                                | [u]                | 3.909              |
| Nominal pressure angle - drive side (°)   | [ $\alpha_{dD}$ ]  | 20.0000            |
| Nominal pressure angle - coast side (°)   | [ $\alpha_{dC}$ ]  | 20.0000            |
| Limit pressure angle (°)                  | [ $\alpha_{lim}$ ] | -1.3577            |
| Generated pressure angle - drive side (°) | [ $\alpha_{nD}$ ]  | 18.6423            |
| Generated pressure angle - coast side (°) | [ $\alpha_{nC}$ ]  | 21.3577            |
| Effective pressure angle - drive side (°) | [ $\alpha_{eD}$ ]  | 20.0000            |
| Effective pressure angle - coast side (°) | [ $\alpha_{eC}$ ]  | 20.0000            |

Figure 3.3-7 Report, information on pressure angles

[See file Exercise-Bevel-03-sizing\\_hypoid\\_face\\_hobbing-v2200-jl-public\\_Step-3.Z70](#)

## 3.4 Step 4

Use the fine sizing function e.g. as shown below. Set parameters as considered suitable and run the fine sizing function:



Look at (as a function of offset, number of teeth on pinion, etc.)

- Efficiency
- Flank strength
- Gear (and hence bearing) forces (radial and axial, typically pinion bearings are more critical)

It is up to the design engineer to now select a suitable solution.

[See file Exercise-Bevel-03-sizing\\_hypoid\\_face\\_hobbing-v2200-jl-public\\_Step-4.Z70](#)